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normal of its $(n - 1)$ -dimensional surfaces. Only the illuminated $(n - 1)$ -dimensional surfaces need to be processed by the algorithm, thereby decreasing the computation time.

Description of the Algorithm

The intersecting shadow volume algorithm is an object-space algorithm. It accepts geometrical and topological descriptions of multiple convex objects and the positions of multiple light sources. The viewer is restricted to the near side of all objects which in turn are restricted to the near side of a background plane whose dimension is one less than the dimension of the scene. Shadows are calculated and added to the scene which is then projected for presentation.

In the accompanying figures, parts of the scene are presented in various colors: black for objects; red for the shadow volume of an object formed by a single light source; blue for the shadow volume of a second light source; and green for the intersection of the illuminated portion of the surface of an object and the shadow volume of another object (i.e., the shadow cast upon the illuminated portion of the first object).

Two Three-Dimensional Objects X and Y and One Light Source L: The algorithm is applied in three steps to determine shadows.

□ *Step 1:* Use normals to separate the surface polygons of a polyhedron into those illuminated by L and those that are not. The illuminated surface of a polyhedron is defined as consisting of all its illuminated surface polygons. The shadow volume of the polyhedron from the light source is generated

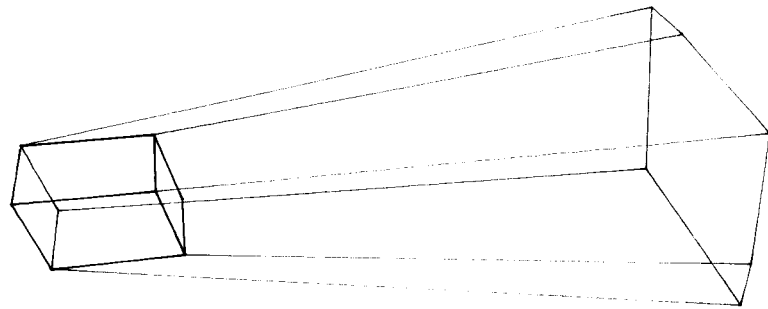


Figure 1: The shadow areas of a polyhedron.

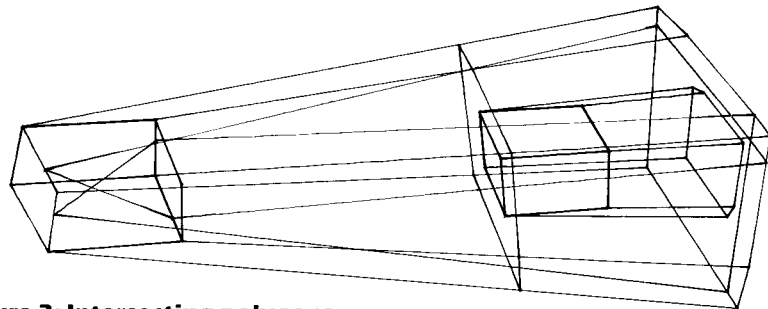


Figure 2: Intersecting polygons attached to the extended surface polygons.

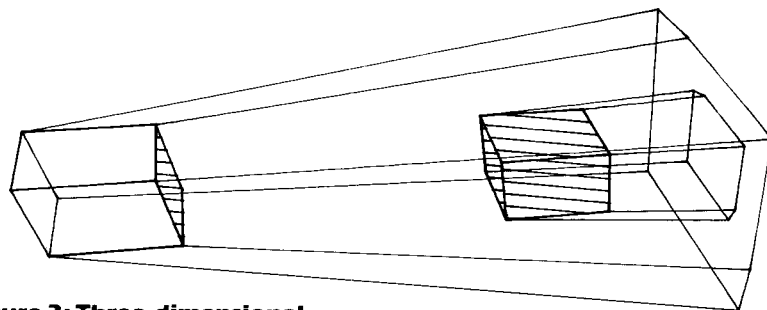


Figure 3: Three-dimensional shadows.

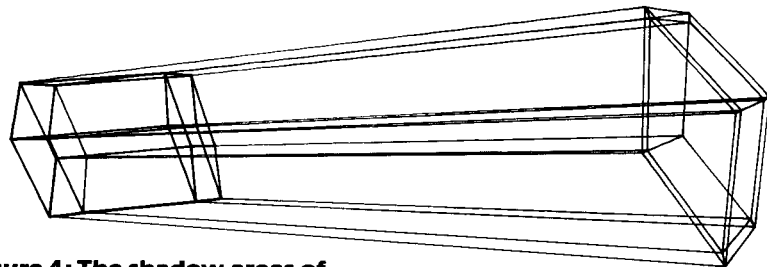


Figure 4: The shadow areas of hyperpolyhedra.

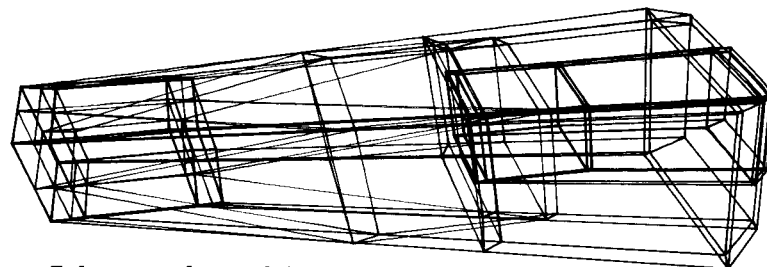


Figure 5: Intersecting polyhedra attached to the extended surface polyhedra.

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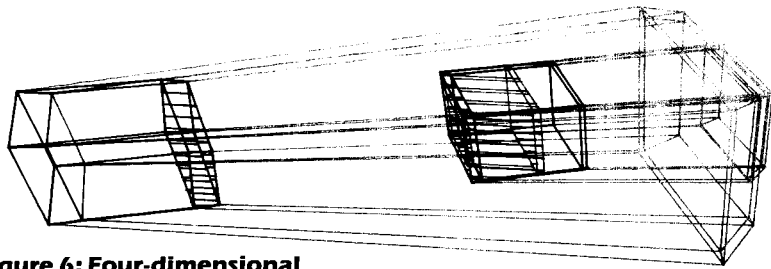


Figure 6: Four-dimensional shadows.

by projecting the illuminated surface from the polyhedron toward the background plane. The shadow volume is itself a three-dimensional polyhedron bounded on the ends by the illuminated surface and the projection of the illuminated surface onto the background plane (Figure 1). This is computationally equivalent to projecting each illuminated surface polygon onto the background plane.

□ *Step 2:* Intersect the shadow volume of polyhedron Y with each illuminated surface polygon of polyhedron X. If the intersection is nonempty, the intersection is a shadow polygon, line, or point and is added to the list of shadows in the scene. Repeat, interchanging the roles of polyhedra X and Y (Figures 2 and 3).

□ *Step 3:* Project and present the illuminated surfaces and shadows (polygons, lines, and points).

Two Four-Dimensional Objects X and Y and One Light Source L: The algorithm is extended to determine shadows in four-dimensional space in three steps.

□ *Step 1:* Use normals to separate the surface polyhedra of the hyperpolyhedron into those illuminated by L and those that are not. The illuminated surface of a hyperpolyhedron is defined as consisting of all its illuminated surface polyhedra. The shadow hypervolume of the hyperpolyhedron from the light source is generated by projecting the illuminated surface from the hyperpolyhedron toward the background hyperplane. The shadow hypervolume is itself a four-dimensional hyperpolyhedron bounded on the ends by the illuminated surface and the projection of the illuminated surface onto the back-

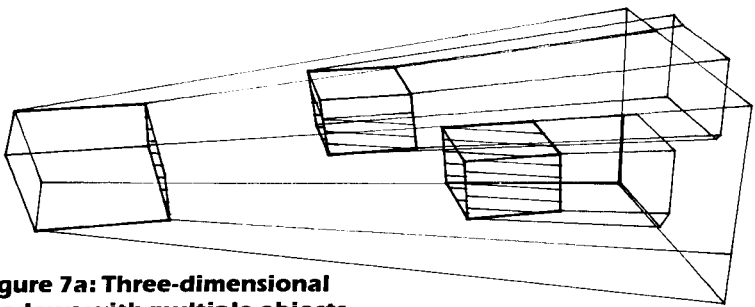


Figure 7a: Three-dimensional shadows with multiple objects.

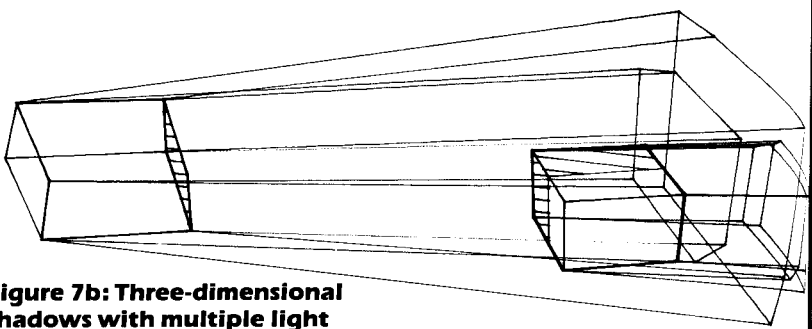


Figure 7b: Three-dimensional shadows with multiple light sources.

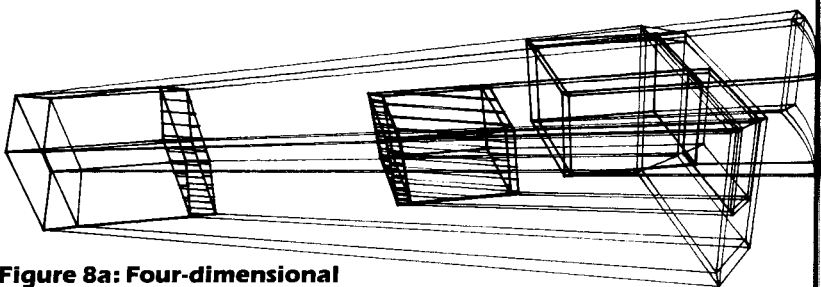


Figure 8a: Four-dimensional shadows with multiple objects.

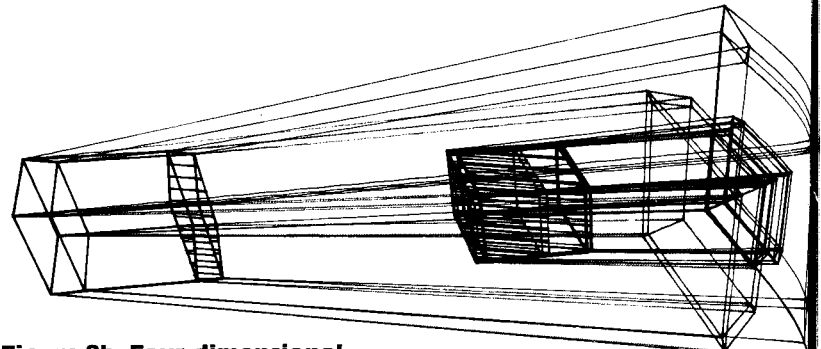
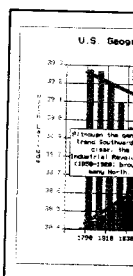


Figure 8b: Four-dimensional shadows with multiple light sources.



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ground hyperplane (Figure 4). This is computationally equivalent to projecting each illuminated surface polyhedron onto the background hyperplane.

□ *Step 2:* Intersect the shadow hypervolume of a hyperpolyhedron Y with each illuminated surface polyhedron of hyperpolyhedron X. If the intersection is nonempty, the intersection is a shadow entity of dimension less than four and is added to the list of shadows in the scene. Repeat, interchanging the roles of hyperpolyhedra X and Y (Figures 5 and 6).

□ *Step 3:* Project and present the illuminated surfaces and shadows (polyhedra, polygons, lines, and points).

Two n-Dimensional Objects X and Y and One Light Source L: The algorithm is applied to determine shadows in n-dimensional space in three steps.

□ *Step 1:* Use normals to separate the (n-1)-dimensional surface elements of the n-dimensional convex object into those illuminated by L and those that are not. The illuminated (n-1)-dimensional surface of the object is the union of its illuminated (n-1)-dimensional surface elements. The shadow hypervolume of the object from the light source is generated by projecting the illuminated surface of the object toward the background hyperplane. The shadow hypervolume is itself an n-dimensional hyperpolyhedron bounded on the ends by the illuminated surface and the projection of the illuminated surface onto the background hyperplane.

□ *Step 2:* Intersect the n-dimensional shadow hypervolume of the object Y with each illuminated

surface element of the object X. If the intersection is nonempty, the intersection is a shadow entity and is added to the list of shadows in the scene. Since the shadow hypervolume is of dimension n and the illuminated surface element is of dimension n-1, the dimension of a shadow entity is at most n-1. Repeat, interchanging the roles of

Determining Object Surface Illumination

An n-dimensional convex object Y is defined by a finite set of linear equations E_1, \dots, E_m as follows. A point $X + (x_1, \dots, x_n)$ of n-space is strictly in Y only if $E_i(x) > 0$ for $i = 1, \dots, m$, (i.e., if the point x is strictly "inside" every hyperplane which defines Y). A point is inside, or on, Y only if $E_i(x) \geq 0$ for $i = 1, \dots, m$.

The convex object Y defined by E_1, \dots, E_m has m (n-1)-dimensional boundary surfaces, each of which lies in one of the m hyperplanes $E_i(x) = 0$. If E_i is the linear equation that defines the i-th (n-1)-dimensional surface element, then the element is illuminated by a light source at the point X only if $E_i(x) > 0$ (i.e., if X is "outside" the boundary hyperplane used to define object Y).

A hyperplane E is defined by first choosing n points p_1, \dots, p_n which do not lie in (n-2)-dimensional space. Each point p_i can be written in terms of its n coordinates as $p_i = (p_{i1}, \dots, p_{in})$, where p_{ij} denotes the projection of p_i on the j-th axis. The $n \times n$ matrix $M = (m_{ij})$ is found next where

$$m_{ij} = \begin{cases} X_j - P_{ij} & \text{if } i = 1, 1 \leq j \leq n \\ P_{ij} - P_{1j} & \text{if } 2 \leq i \leq n, 1 \leq j \leq n \end{cases}$$

The linear equation E is the determinant of the matrix M. It can be given in the ordinary linear form

$E(x) = C_1 x_1 - C_i P_{1i}$, where C_i is the cofactor of the element in the first row and i-th column of the matrix M. ■

the n-dimensional objects X and Y. □ *Step 3:* Project and present the illuminated surfaces and shadows (which are at most (n-1)-dimensional).

Multiple Objects and Light Sources: If there are m n-dimensional objects X_1, X_2, \dots, X_m in the scene with V_1, V_2, \dots, V_m illuminated surface elements respectively, then Step 2 of the algorithm is repeated for each illuminated surface element of the hyperpolyhedron for each of the m n-dimensional shadow volumes. Assuming the average number of visible surface polyhedra to be V , the computational time of the algorithm is increased by a factor of $(m-1)V$.

If there are k light sources L_1, \dots, L_k , then Step 2 of the algorithm must be repeated k times. This increases the computation time of the algorithm by a factor of k.

Assuming k light sources and m objects with the same average number of illuminated surfaces, the total computation time—including transformations, hidden-surface elimination, calculation of shadow volumes, intersections and shadows cast upon objects—another $kn(n-1)t_a v$, where $t_a v$ is the average computation time to calculate shadows cast upon one object from another.

Running on a VAX 11/750, the computation time to calculate typical three- and four-dimensional shadows is listed in Table 1.

Conclusion

The shadow algorithm presented here has been successfully implemented to determine shadows in three- and four-dimensional space. Multiple objects (Figures 7a and b) and multiple light sources (F



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Calculation of the Point(s) of Intersection of a Line and an m-dimensional Subspace in n-space, m < n

To determine what parts of an illuminated (n - 1)-dimensional surface lie in an n-dimensional shadow volume, it is necessary to break down the illuminated surface into its line elements and then determine the intersection of the line elements of the illuminated surface and the (n - 1)-dimensional boundaries of the shadow volume. Thus, the problem of the intersection of a line and an m-dimensional space where m < n needs to be solved.

A line L (a one-dimensional space) is defined by two points 1₁ and 1₂ where (1₁₁, 1₁₂, ..., 1_{1n}) are the n-space coordinates of the point 1₁. A point x = (x₁, ..., x_n) is on L only if x_i = t(1_{1i} - 1_{2i}) + 1_{2i} for some real number t and for all i, 1 ≤ i ≤ n.

An m-dimensional space S is defined by m + 1 points s₁, ..., s_{m+1}. By an appropriate change of coordinates, it is assumed, without loss of generality, that the 1-dimensional space L and the m-dimensional space S lie in a space spanned by the first (m + 1)-coordinate axis of n-space. Since S is confined to the (m + 1)-dimensional subspace in the first (m + 1) space coordinates, the space S may be given as the solution of S(x) = 0 where

$$(1) S(x) = B_j(x_j - s_{1j}),$$

where B_j is the determinant of the m × m matrix

$$b_{11} \dots b_{1,j-1} b_{1,j+1} \dots b_{1,m+1}$$

⋮

$$B_j = b_{11} \dots b_{1,j-1} b_{1,j+1} \dots b_{1,m+1}$$

⋮

$$b_{m1} \dots b_{m,j-1} b_{m,j+1} \dots b_{m,m+1}$$

and b_{ji} = s_j + 1 i - s_{1i}.

Since L is confined to an (m + 1)-dimensional space in the first (m + 1) space coordinates, the previous remark can be refined to state that x belongs to L only if x_j = t(1_{1j} - 1_{2j}) + 1_{2j} for some real number t for all j, 1 ≤ j ≤ m + 1 and x_j = 1_{2j} = 1_{1j} for all j, m + 2 ≤ j ≤ n.

Let A_j = 1_{1j} - 1_{2j}, 1 ≤ j ≤ m + 1. Since 1₁ ≠ 1₂, there is an index, say i, such that A_i ≠ 0. The equation x_j = tA_j + 1_{2j} is multiplied by A_i, and the equation x_i = tA_i + 1_{2i} is multiplied by A_j, and then subtracted. Then

$$A_j x_i - A_i x_j = A_j 1_{2i} - A_i 1_{2j} f_j,$$

which can be rewritten as

$$x_j = (A_j x_i - f_j) / A_i.$$

Thus, a point x = (x₁, ..., x_n) belongs to L only if

$$x_j = (A_j x_i - f_j) / A_i, \quad 1 \leq j \leq i-1$$

$$x_i = tA_i + 1_{2i}, \quad j = i$$

(2)

$$x_j = (A_j x_i - f_j) / A_i, \quad i+1 \leq j \leq m+1$$

$$x_j = 1_{2j} = 1_{1j}, \quad m+1 \leq j \leq n.$$

Assume that L and S intersect. Let x be a point both on L and in S. Since x is on L, x satisfies (2). Since x is in S, S(x) = 0. Using (1),

$$(3) B_j(x_j - s_{1j}) = 0.$$

Then (3) is rewritten as

$$(4) B_j x_j = B_j s_{1j}$$

and (2) is substituted in (4):

$$(5) B_j x_i + B_j (A_j x_i - f_j) / A_i = B_j s_{1j}.$$

Multiplying by A_i, equation (5) becomes

$$(6) (B_j A_i) x_i = A_i B_j s_{1j} + B_j f_j.$$

If B_jA_i = 0, then there is no restriction on x_i and the entire line L in in the subspace.

If B_jA_i ≠ 0, then the point x_i is uniquely defined by

$$(7) x_i = [A_i B_j s_{1j} + B_j f_j] / (B_j A_i).$$

Since x_i is uniquely defined by (7), then all the other coordinates of x are uniquely defined by (2). In this case, the point of intersection has been computed. ■

ures 7b and 8b) have been included in scenes. The objects used in three-dimensional scenes are cubes; the objects used in four-dimensional scenes are hypercubes.

When the shadows in a four-dimensional scene overlap each other it has been difficult to tell where each shadow is actually located. As a means of increasing the realism of the scene, depth cues to achieve realism in a three-dimensional scene should be considered. These might include rotation, hidden-surface elimination, interaction and stereoscopy. It is still difficult to predict that a profound feeling of hyperspace will be gained. Nevertheless, the development of a shadow algorithm for hyperspace represents one more step toward the threshold beyond which an intuitive feeling for hyperdimensional scenes will be realized.

Some of the numerical algorithms needed for the implementation of the shadow algorithm accompany this article. A complete description of the numerical algorithms is available in Mei-chi Li Master's Thesis (see References

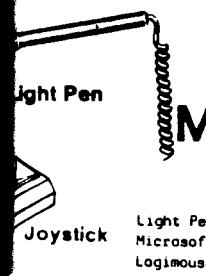
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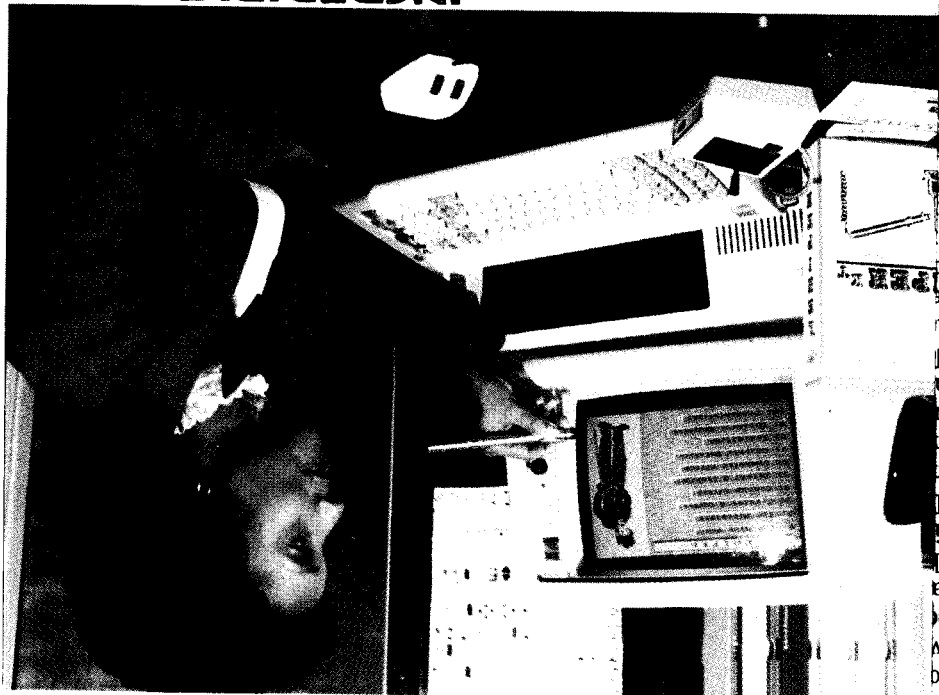
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Douglas Campbell is a Professor of Computer Science at Brigham Young University. He received a Ph.D. in Mathematics from the University of North Carolina in 1971.

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Robert Burton is a Professor of Computer

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have been included in the four-dimensional cubes are used in the objects used in the four-dimensional cubes. adows in a four-dimensional space. The intersection, hidden surface, and interaction, is still difficult to find. A profound feeling of depth is gained. The development of a shadow algorithm for the implementation of a numerical article. A comprehensive numerical article in Mel-chi Liu's Hyperdimensional Graphics & Animation. (see Reference)