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# Experimental nonlocal and surreal Bohmian trajectories

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at first deemed "surreal" when the second particle is used to probe the position of the first particle. We entangle two photons and determine a set of Bohmian trajectories for one of them using weak measurements and postselection. We show that the trajectories seem surreal only if one ignores their manifest nonlocality.

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Keywords: weak measurement, quantum measurement, Bohmian mechanics, interpretations of quantum mechanics

# INTRODUCTION

The concept of a trajectory, the path followed by a particle, is ubiquitous in classical mechanics. In orthodox quantum mechanics, however, a particle does not follow a trajectory, because it does not have a simultaneous position and momentum. Nonetheless, it is possible to reinterpret the quantum formalism as describing particles following definite trajectories, each with a precisely defined position at each instant in time. However, in this interpretation, called Bohmian mechanics (1-4), or the de Broglie-Bohm interpretation (5, 6), the trajectories of the particles are quite different from those of classical particles, because they are guided by the wave function. This allows for phenomena such as double-slit interference, as has been investigated experimentally for single photons (7). Note that this is very different from the Feynman path formalism of quantum mechanics (8), where the transition probability between two points in phase space is calculated using all possible paths between those two points. In contrast to the Feynman formalism, Bohmian mechanics says that each quantum particle in a given experiment follows a trajectory in a deterministic manner. Thus, much of the intuition of classical mechanics is regained.

As with any interpretation of quantum mechanics, the experimental predictions of Bohmian mechanics are the same as those in the operational theory. The stochastic nature of measurement outcomes for which quantum mechanics is famous is ascribed to ignorance about the initial configuration of the particle(s) in the experiment, an uncertainty that is described precisely by the wave function prepared by the experimenter (1-4, 6, 9). This tidily allows features of operational quantum theory, such as the Heisenberg uncertainty principle, to be explained within the Bohmian formalism. A consequence of this is that the trajectory of a single Bohmian particle cannot be observed in an experiment on that particle; any measurement of a particle's position changes the wave function and thus the quiding notential that the particle experiences. Note that this change

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measurement of the momentum of a particle at a given instant in time. The weakness ensures that the system is not disturbed appreciably, so that it is sensible to make a subsequent measurement of position. Repeating the experiment many times, one can calculate the average momentum as a function of position. This entire process can then be repeated at many instants in time, allowing a set of average trajectories to be reconstructed. It was shown by Wiseman (9) how these trajectories, in the limit of very weak measurements, correspond exactly to the trajectories obtained from the Bohmian interpretation.

To explain nonlocal phenomena such as Bell nonlocality (10), any realistic interpretation of quantum mechanics must also be nonlocal, and Bohmian mechanics is no exception (2). This can be seen in the Bohmian velocity law (shown later), where the velocity of a particle can depend explicitly on the position of a second particle, even when the particles are far apart and not interacting by any conventional mechanism and even though the second particle may be influenced, independently of the first particle, by the apparatus chosen by the experimenter.

Here, as proposed by Braverman and Simon (11), we experiment on two entangled particles (photons) and map out the trajectories of one of them as it traverses a double-slit apparatus. We show that the trajectories of this first particle (and therefore both its position and its velocity) are indeed affected by an externally controlled influence on the distant second particle. For some choices of that control, the second particle in our experiment can be used to determine through which slit the first particle has gone. Englert, Scully, Süssmann, and Walther (ESSW) (12) asserted that in the presence of such a Welcher Weg measurement (WWM) device, the particle's Bohmian trajectories can display seemingly contradictory behavior: There are instances when the particle's Bohmian trajectory goes through one slit, and yet the WWM result indicates that it had gone through the other slit. ESSW concluded that these trajectories predicted by Bohmian mechanics could not correspond to reality and they dubbed them "surreal trajectories." This serious assertion was discussed at length in the literature (13–17), after which a resolution of this seeming inconsistency was proposed by Hiley et al. (18). Here, we present an experimental validation of this resolution, in which the nonlocality of Bohmian mechanics comes to the fore.

# **THEORY**

The de Broglie-Bohm dynamics can be formulated in a number of different ways (1, 3-6, 9). Here, we present the formulation that is simplest and most appropriate to our method of empirical determination via weak values (4, 9). Being a complete interpretation of quantum mechanics, Bohmian mechanics applies to arbitrarily many particles and allows for internal degrees of freedom (such as spin). Here we are concerned with a two-particle entangled state IV). Denoting the

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where  $\hat{v}_1 = (\hat{p}_1/m_1)$  is the velocity operator for particle 1.

The existence of entanglement entails counterintuitive effects in Bohmian mechanics, which ESSW used to attack the foundations of the theory as follows. Consider an experiment where a particle traverses a double-slit apparatus, thus preparing it in a state described by the double-slit wave

function,  $\psi(x_1; t=0) = \frac{1}{\sqrt{2}}(\psi_u(x_1; 0) + \psi_l(x_1; 0))$ . Here, the two wave functions  $\psi_u(x_1; t)$  and  $\psi_l(x_1; t)$  describe symmetric single-slit wave functions for slits centered at  $x_1 = d/2$  and  $x_1 = -d/2$ , the specific form of which is not necessary for this discussion. Now, say the apparatus includes a WWM device—another quantum system that acts as a qubit memory, storing the single bit of information about which slit the particle goes through. This can be modeled by the following joint state of the double-slit particle and the WWM device at times t > 0

$$|\Psi(t)\rangle = \frac{1}{\sqrt{2}} \int dx_1 dx_2 |x_1\rangle |x_2\rangle [\Psi_u(x_1;t)\phi_H(x_2;t)|H\rangle + \psi_1(x_1;t)\phi_V(x_2;t)|V\rangle]$$
 (2)

Here, the WWM device is described as a particle with a spin degree of freedom, denoted (with forethought of the experiment described later in this text) by the kets  $|H\rangle$  and  $|V\rangle$  and a position  $x_2$ . The spin degree of freedom provides the qubit that stores the WWM information, and the two states are correlated with the wave function for particle 1 initially localized at the upper and lower slit, respectively. The reason for choosing a spin degree of freedom for this role is that, unlike position, spin has no autonomous hidden variable assigned to it in standard Bohmian mechanics. [In some extensions to Bohmian mechanics, autonomous hidden variables are assigned to degrees of freedom other than position, such as spin (19). See Hiley and Callaghan (20) for a discussion in the context of the original ESSW proposal. To avoid the surreal trajectories of ESSW in the scenario we are considering, the hidden variable theory would have to assign a value to the particular spin observable with  $|H\rangle$  and  $|V\rangle$  as its eigenstates.] That is, Bohmian mechanics does not necessarily ascribe a definite value to the bit (H or V) storing the WWM information, and this is essential to the ESSW phenomenon. However, the position  $x_2$  of particle 2 (which is ascribed a value in Bohmian mechanics) can be used to "read out" this WWM information, by sending particle 2 to different detectors depending on its spin state. Because these two states are orthogonal ( $\langle H|V\rangle = 0$ ), it would be intuitive to conclude that such a measurement of the spin of particle 2 would indicate through which slit particle 1 had gone (even though, in orthodox quantum mechanics, the particle has no trajectory and hence did not "go through" either slit).

In some situations, Bohmian mechanics accords with that intuition. If the WWM is read out as described above, at time  $t_r > 0$ , then for times  $t < t_r$ ,  $\phi_H(x_2; t)$  and  $\phi_V(x_2; t)$  are identical, whereas for times  $t > t_r$ ,  $\phi_H(x_2; t)$  and  $\phi_V(x_2; t)$  have disjoint support. If, at the time  $t_r$ , particle 1 is still in the near

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 $\text{gives} \overset{\text{Re}}{=} \left[ \frac{-i\hbar \psi_{\mathrm{u}}'(x_{\mathrm{l}};t)}{m\psi_{\mathrm{u}}(x_{\mathrm{l}};t)} \right]_{\text{Or}} \overset{\text{Re}}{=} \left[ \frac{-i\hbar \psi_{\mathrm{l}}'(x_{\mathrm{l}};t)}{m\psi_{\mathrm{l}}(x_{\mathrm{l}};t)} \right]_{\text{respectively, as expected from single-particle Bohmian}$ mechanics.

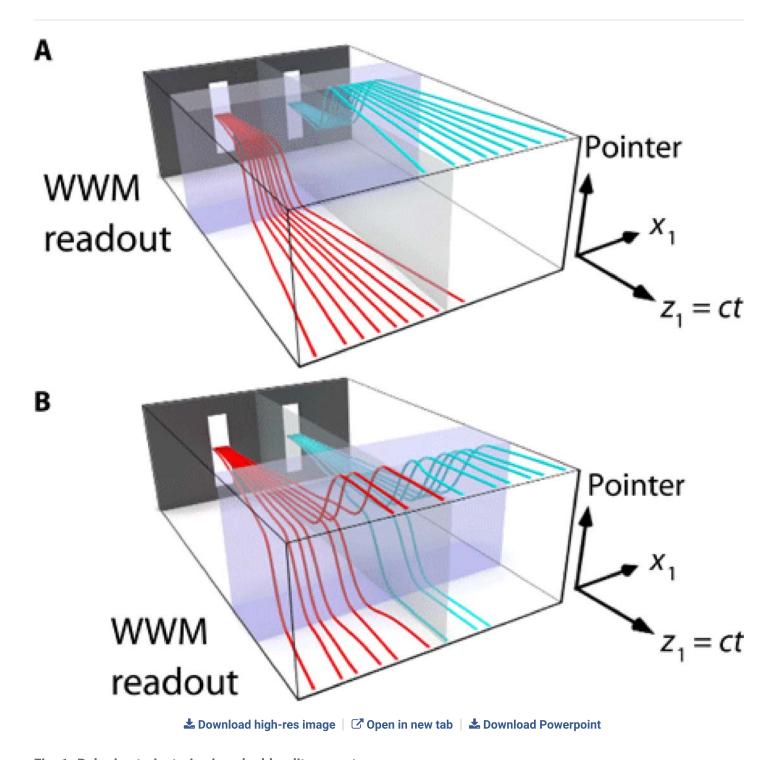


Fig. 1 Bohmian trajectories in a double-slit apparatus.

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diagram. Near the line of symmetry of the apparatus, both outcomes of the WWM are equally likely, regardless of which slit the Bohmian trajectory originates from.

ESSW, however, consider a situation where the readout via the position of particle 2 does not take place until after particle 1 has traversed the double-slit apparatus into the far field. In this case, while particle 1 traverses the apparatus,  $\phi_H(x_2;t) = \phi_V(x_2;t)$  and the velocity formula (**Eq. 1**) is independent of  $x_2$ 

$$v_1(x_1;t) = \frac{\hbar}{m} \operatorname{Im} \left[ \frac{\psi_u^*(x_1;t)\psi_u'(x_1;t) + \psi_1^*(x_1;t)\psi_1'(x_1;t)}{|\psi_u(x_1;t)|^2 + |\psi_1(x_1;t)|^2} \right]$$
(3)

This function is odd in  $x_1$  because  $\psi_u(-x_1;t) = \psi_l(x_1;t)$ , for all t, by construction. Furthermore, the one-dimensional trajectories defined by using this velocity cannot cross because the velocity field is single-valued in  $x_1$ . A consequence of these two properties is that no trajectory can cross the  $x_1 = 0$  line. Thus, Bohmian mechanics in this situation predicts that, when particle 1 is detected in the far field, if  $x_1 > 0$ , then it must have come from the upper slit, and if  $x_1 < 0$ , then it must have come from the lower slit. Moreover, one can show that, in the far field, the position of particle 1 is almost completely uncorrelated with the spin of particle 2. Thus, upon detection of particle 1 anywhere in the far field, a measurement of particle 2 can yield either  $|H\rangle$  or  $|V\rangle$ . A conceptualization of this is displayed in **Fig. 1B** in which the WWM readout actually occurs in the midfield for clarity. The trajectories corresponding to the measurement outcomes are "surreal" in the sense that the orthodox quantum intuition is that particle 2 should reliably carry the WWM information about which slit particle 1 "actually" went through, and yet we find that the trajectories predicted by Bohmian mechanics often fail to agree with the outcome of the WWM as read out via particle 2.

The resolution [presented by Hiley et al. (18)] of the apparent paradox is in the nonlocality of Bohmian mechanics. In Bohmian mechanics, the spin of particle 2 is described by a Bloch vector  $\mathbf{s}_2$  that depends on the actual position of the two particles (21) in a manner exactly analogous to Eq. 1

$$\mathbf{s}_{2}(x_{1}, x_{2}; t) = \frac{\langle \Psi(t) | \widehat{\mathbf{s}}_{2} | x_{1} \rangle | x_{2} \rangle \langle x_{1} | \langle x_{2} | \Psi(t) \rangle}{\langle \Psi(t) | x_{1} \rangle | x_{2} \rangle \langle x_{1} | \langle x_{2} | \Psi(t) \rangle} \tag{4}$$

where  $\hat{\mathbf{s}} = (\sigma_x, \sigma_y, \sigma_z)$ . We define  $|H\rangle$  and  $|V\rangle$  to be eigenstates of  $\sigma_z$  with eigenvalues +1 and -1, respectively. Then, for the situation of **Fig. 1A**, **Eq. 4** evaluates to  $(1, 0, 0)^T$  or  $(-1, 0, 0)^T$ , depending on which slit particle 1 went through. For the situation in **Fig. 1B** (a delayed measurement), it evaluates to

$$\mathbf{s}_{2}(x_{1}, x_{2}; t) = \frac{(\psi_{\mathbf{u}}^{*}(x_{1}; t)\langle H| + \psi_{\mathbf{l}}^{*}(x_{1}; t)\langle V|)\widehat{\mathbf{s}}_{2}(|H)\psi_{\mathbf{u}}(x_{1}; t) + |V\rangle\psi_{\mathbf{l}}(x_{1}; t))}{(5)}$$

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through. Similar unreliable behavior can result if the Welcher Weg information were stored in disjoint positional wave functions of the second particle, if those two wave functions are subsequently allowed to overlap, as in the experiment proposed by Braverman and Simon (11).

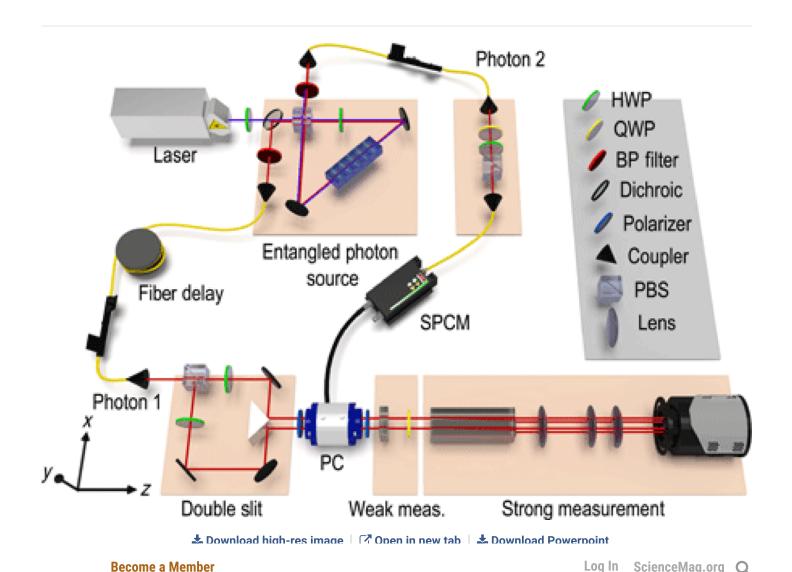
## **EXPERIMENT**

Here, we perform an experiment using the spin of particle 2 as carrier of the Welcher Weg information, as per the above theory. We determine the trajectories of particle 1 in an operational manner that does not rely on a particular interpretation of quantum mechanics (9), as realized by Kocsis et al. (7), using weak measurements of velocity postselected on the positions of the particles. The particles in this article are photons, as was the case in Kocsis et al. (7). Bohmian-like trajectories of massless spin 0 and spin 1 particles have been studied (22), but in the case of this experiment, we instead make use of the equivalence between the one-dimensional Schrodinger equation and the two-dimensional Helmholtz equation in the paraxial approximation. The evolution of the transverse position x and momentum  $k_x$  of a single photon propagating close to the z direction has an exact mathematical correspondence with the quantum theory of a nonrelativistic particle of mass  $m = \hbar\omega/c^2$  propagating in one dimension with position x and momentum  $p = \hbar k_x$ .

As described previously, the mapping out of a set of possible Bohmian trajectories for a particle requires a measurement of momentum followed by a measurement of position, repeated many times (that is, using an ensemble of identically prepared systems) to obtain averages, and repeated at many instants in time to connect the trajectory segments. It is the measurement of both position and momentum that makes mapping out the set of trajectories challenging: Quantum mechanics tells us that any measurement of momentum will necessarily disturb the position of the particle being measured. To circumvent this, we measure the momentum in such a way that a single shot vields virtually no information and causes virtually no disturbance, so that the subsequent strong measurement of position reveals [in the Bohmian interpretation (4)] the Bohmian position of the particle at the point where its momentum was measured (4, 9). Because the signal-to-noise ratio in any individual momentum measurement is so small, it is necessary to use a very large ensemble to obtain reliable averages. This technique of averaging such weak measurement results to obtain a so-called weak value (23) has been important in fundamental quantum experiments, including probing Hardy's Paradox (24, 25), testing measurement-disturbance and complementarity relations (26-29), demonstrating violation of macrorealism (30, 31), and elucidating Feynman's explanation of Bell correlations (32). It is not immediately obvious that this measurement will tell us anything about the Bohmian velocity of the particle being measured, because this velocity does not have the same statistics as the quantum mechanical momentum (divided by m). Nonetheless, it can be shown that

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As stated, the particles in our experiment are photons and, in reference to the theory presented above, the spin operator  $\hat{\mathbf{s}}$  corresponds to their polarization, with  $\sigma_z$  being diagonal in the H/V basis. The experimental apparatus is depicted in **Fig. 2**. We generate polarization-entangled photon pairs via type II downconversion (for details, see Materials and Methods). Photon 1 is sent through a 50-m-long single-mode fiber to a double-slit apparatus. The photon's wave function is prepared in a double-slit superposition using a polarizing beamsplitter and a pair of prism mirrors, such that if the polarization of photon 1 is horizontal, it is prepared in the upper slit wave function, whereas if it is vertical, it is prepared in the lower slit wave function. These virtual slits are separated by 2.61 mm, and each has a root mean square width of 0.55 mm. The polarization of the photons in both paths is made the same,  $|D\rangle = \frac{1}{\sqrt{2}}(|H\rangle + |V\rangle)$ , by a set of half waveplates and a polarizer. Because of the initial polarization entanglement, the path of photon 1 is now entangled with the polarization of photon 2, as described in **Eq. 2**.



A Sagnac interferometer-based source of entangled photons prepares two photons in a maximally entangled state that are then spectrally filtered using two band-pass (BP) filters. Photon 1 is sent into a double-slit apparatus and immediately split at a polarizing beamsplitter (PBS) to prepare the double-slit wave function. The lower arm's polarization is changed to match the upper arm using a half waveplate (HWP). Both upper and lower arms passed through a polarizer, a Pockels cell (PC), and another polarizer, to postselect upon the detection of photon 2. The transverse velocity of photon 1 is weakly measured using a 0.7-mm-thick piece of calcite with its optic axis oriented at 42° to the normal in the horizontal plane, followed by a quarter waveplate (QWP) and a beam displacer. Finally, the wave function of photon 1 is imaged in different planes using an imaging system composed of three lenses, and its position is measured using a single-photon cooled CCD. Photon 2 is sent through an HWP and a QWP, followed by a PBS to measure its polarization in different bases.

To perform a WWM on photon 1, we measure the polarization of photon 2 using a set of waveplates and polarizing beamsplitters. For details on how we perform measurements on photon 1 using a charge-coupled device (CCD) camera, in coincidence with measurements on photon 2, see Materials and Methods. Next, we weakly (23, 33) measured the velocity  $v_1 = ck_x/|\mathbf{k}|$  of photon 1, before strongly measuring its position. To weakly measure the transverse velocity of photon 1, we coupled the k vector of photon 1 to its polarization using the angle-dependent birefringent phase shift produced by a piece of calcite (7) that is thin enough that spatial walk-off of the beam inside the crystal is negligibly small, but thick enough that the polarization rotation that the beam undergoes is measurable. The crystal's optic axis was oriented in the horizontal plane; hence, photons with different transverse velocities experienced different indices of refraction and therefore received different phase shifts. The phase shift is well approximated over our range of incident angles (transverse momenta) by the linear expansion

(6)

where the dimensionless coupling strength, ζ, was determined to be 550.2 ± 0.96. This momentumdependent phase shift serves to weakly correlate the photon's momentum with its polarization. By measuring the polarization, a weak measurement of momentum is thus performed. The photon's polarization was measured in the right-hand circular (R)/left-hand circular (L) basis [] using a quarter waveplate oriented at 45° and a beam displacer, the combination of which displaces the L-polarized beam vertically relative to the R. Using this polarization measurement, the photon's weak-valued velocity takes on a particularly simple form (7)

(7)

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## RESULTS

In Fig. 3, we demonstrate the nonlocality present in Bohmian mechanics by showing that the trajectory of photon 1 is affected by the remote choice of how to measure photon 2. We measure the polarization of photon 2 in two different bases and postselect the measurement outcomes of photon 1 on a particular result, as described above. Defining states, the two different bases are {|  $\psi^0\rangle \ \ , |\psi^\pi\rangle \ \ \} \ \text{and} \ \{|\psi^{\pi/2}\rangle \ \ , |\psi^{3\pi/2}\rangle \ \ \}. \ \text{All four final states} \ |\psi^\Phi\rangle \quad \text{are equally likely, and for each, we}$ measure the set of trajectories that photon 1 follows. In this way, it is possible to plot a single trajectory beginning with the same initial conditions and show that the path depends on the choice of distant measurement. For clarity, the measured weak velocity distribution of photon 1 is also plotted in two planes to show the effect the postselection of photon 2 has on the motion of photon 1. Thus, one can see that even though the position of a particle is a locally defined hidden variable in Bohmian mechanics, the guiding equations that determine its possible trajectories are nonlocal.

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Fig. 3 Observation of nonlocality in Bohmian mechanics.

(A) The reconstructed trajectories when photon 2 is found in the state. The trajectories are drawn over a range of z = 1.7 m to z = 5.9 m, using 67 different planes. The state of photon 1 after postselection contains no information about the state of photon 2, and thus, interference is observed. (B) A single postselected trajectory beginning at the same initial condition, x = -1.12 mm, for four different postselected polarization states of photon 2, , where  $\Phi$  $\in \{0, \pi/2, \pi, 3\pi/2\}$ . The pairs  $\{0, \pi\}$  and  $\{\pi/2, 3\pi/2\}$  correspond to measuring the polarization of photon 2 in two different bases. (Inset) The weak velocity values measured at z = 1.8 m and z = 5.9 m. The velocity distributions are initially independent of phase shift applied to photon 2 but depend strongly on it in the far field. The error bars on the individual velocity measurements are consistent with the scatter observed but are not displayed because they detract from rather than enhance its clarity.

Next, we aim to demonstrate the surreal behavior discussed by ESSW. We measure the trajectories of photon 1 without performing a postselection on photon 2. In this way, the position  $x_2$  of photon 2 is uncorrelated with its polarization, giving Eq. 3 for the velocity of photon 1. To reject spurious background sources of photons, we actually do postselect on detecting photon 2, but we average over the two cases H and V by the weights with which these two outcomes occur (which are close to one-half). In fact, we get the same result regardless of the basis in which we measure the polarization of photon 2; thus, we average the data from three different bases,  $|D/A\rangle$ ,  $|R/L\rangle$ , and

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Because each Bohmian trajectory originates from one or the other slit, these trajectories demonstrate the surreal behavior predicted by ESSW.

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Fig. 4 Observation of surreal trajectories.

(A) The set of reconstructed trajectories for photon 1 without postselection onto a particular polarization of photon 2, corresponding to the delayed WWM of ESSW. The trajectories are plotted over the range z = 1.7 m to z = 5.9 m, using 67 different planes. A single trajectory beginning at x = -0.98 mm is plotted with a thicker, colored line. (B) The polarization of photon 2, represented by its Bloch vector, as a function of the position of photon 1 as it traverses the colored trajectory plotted in (A). The polarization of photon 2 is calculated by performing quantum state tomography (34) on photon 2 and correlating those counts with the counts observed on the single-photon camera. The photons have been entangled such that if photon 1 were to be found in the lower slit, photon 2 would be vertically polarized. This is the case at the start of the single trajectory we consider. However, as photon 1 traverses the double slit, it enters a region where the wave function emanating from the upper slit (for which photon 2 is horizontally polarized) interferes with that from the lower slit, leading to nonlocal coupling between the motion of photon 1 and the polarization of photon 2. As a consequence, the polarization of photon 2 changes over time and its final state no longer faithfully records the WWM information about photon 1.

The apparent contradiction, however, is resolved by also measuring the polarization of photon 2 as a function of the position of photon 1. The measurements that we have performed on photon 2 ( $|D/A\rangle$ ,  $|R/L\rangle$ , and  $|H/V\rangle$ ), in correlation with the measurement of the position of photon 1, are sufficient to perform quantum state tomography (34) on the polarization of photon 2, along a trajectory of photon 1. Unlike the case of Eq. 1, it is not necessary to use a weak measurement of  $\hat{\mathbf{s}}_2$  to determine Eq. 4, because  $\hat{\mathbf{s}}_2$  commutes with the position of all particles at all times. Hence, we can make a strong measurement of the polarization of particle 2, in the three directions (in different runs), conditioned on finding particle 1 at particular positions at particular times. The results of this measurement are plotted in Fig. 4. As a function of the progress of photon 1 along any trajectory that it may follow, the state of photon 2 changes. Initially, for a trajectory originating in the lower slit, photon 2 is found to be vertically polarized (indicating that the outcome of the WWM was "lower slit"). Further along this trajectory, the polarization of photon 2 gradually becomes less vertically polarized and ends up with polarization close to  $|D\rangle$  (see Fig. 4). Thus, a WWM in the H/V basis (or "upper"/"lower" basis) for this photon, at this time, is equally likely to indicate that it came from the upper slit as from the lower slit.

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the upper or the lower slit. However, this surreal behavior is merely the flip side of the nonlocality we also demonstrated. In **Fig. 3**, we showed that the trajectory of photon 1 depends on the choice of measurement (polarization basis) for photon 2. In **Fig. 4**, we see that the polarization of photon 2 depends on the choice of when (that is, at what point along the trajectory) to measure the position of photon 1. This nonlocality is due to the entanglement of the two photons, which, in Bohmian mechanics, makes their evolution inseparable even when the photons themselves are separated. Because entanglement is necessary for the delayed measurement scenario of ESSW, this nonlocal behavior is to be expected and is the reason for the surreal behavior they identify. Indeed, our observation of the change in polarization of a free space photon, as a function of the time of measurement of a distant photon (along one reconstructed trajectory), is an exceptionally compelling visualization of the nonlocality inherent in any realistic interpretation of quantum mechanics.

## MATERIALS AND METHODS

To generate entangled photon pairs, we used a periodically poled KTP (potassium titanyl phosphate) crystal embedded in a polarization Sagnac interferometer (35–37). The source generates entangled photon pairs (at a rate of approximately 25,000 pairs/s and a coupling efficiency of ~10%) in a state  $|\phi^{+}\rangle = \frac{1}{2}(|HH\rangle + |VV\rangle)$ 

ρ that has fidelity  $F = \langle \phi^+ | \rho | \phi^+ \rangle = 99.04 \pm 0.02 \%$  with the Bell state  $| \phi^+ \rangle = \frac{1}{\sqrt{2}} (|HH\rangle + |VV\rangle)$ , where H and V correspond to horizontal and vertical polarization, respectively.

To perform measurements on photon 1 in coincidence with measurements on photon 2, we triggered a Pockels cell to block photon 1 unless photon 2 was detected. The Pockels cell is set to apply a  $\pi$  phase shift to the vertical polarization upon receiving a TTL (transistor-transistor logic) pulse from the single-photon counter. This phase shift converts the polarization of photon 1 from

 $|D\rangle$  to  $|A\rangle = \frac{1}{\sqrt{2}}(|H\rangle - |V\rangle)$ , allowing it to pass through a polarizer following the cell. That is, the detection of photon 2 effectively opens a fast shutter for photon 1, enabling coincidence detection on the nanosecond time scale using a single-photon cooled CCD (Andor iDus) whose response time is six orders of magnitude slower.

To obtain the data for the trajectories, photon 1 was imaged in different planes using two fixed lenses (with focal lengths of 10 and 15 cm) and a third translatable lens (with a focal length of 2.5 cm) in between them. The magnification and imaging distance of the imaging system (consisting of the three lenses and the CCD camera) were determined by sweeping the position of the middle lens with one slit blocked and the weak measurement calcite removed. The magnification of the system

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beam propagation equations. Note that because Bohmian trajectories do not cross in one dimension, these propagation equations also relate the Bohmian position of the particle at the plane where the momentum measurement was performed with that in the plane where it was imaged.

Correction: Equation 3 has been updated.

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