

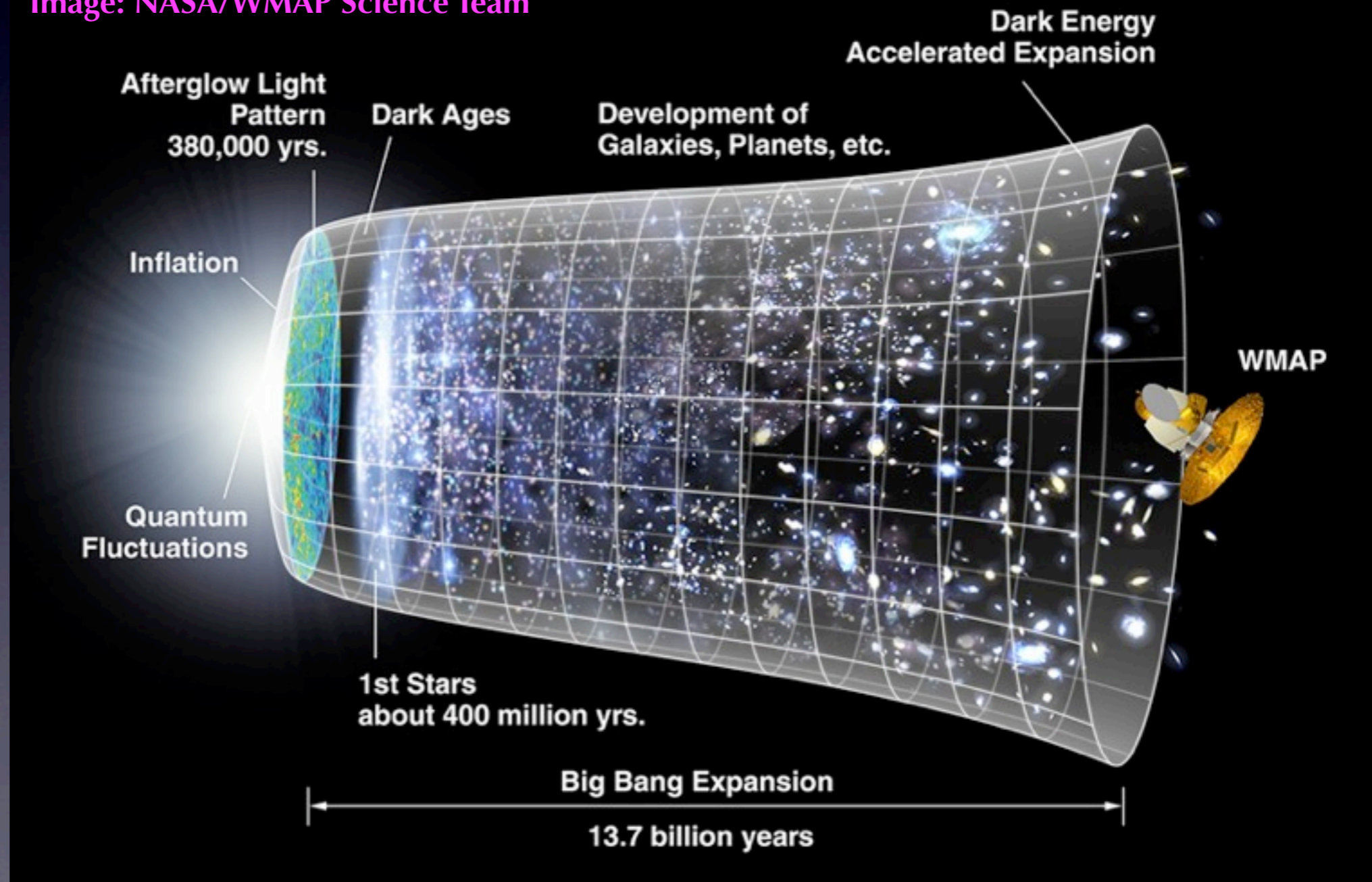
Inflation 2010

US

University of Sussex

Andrew Liddle
January 2010

Image: NASA/WMAP Science Team



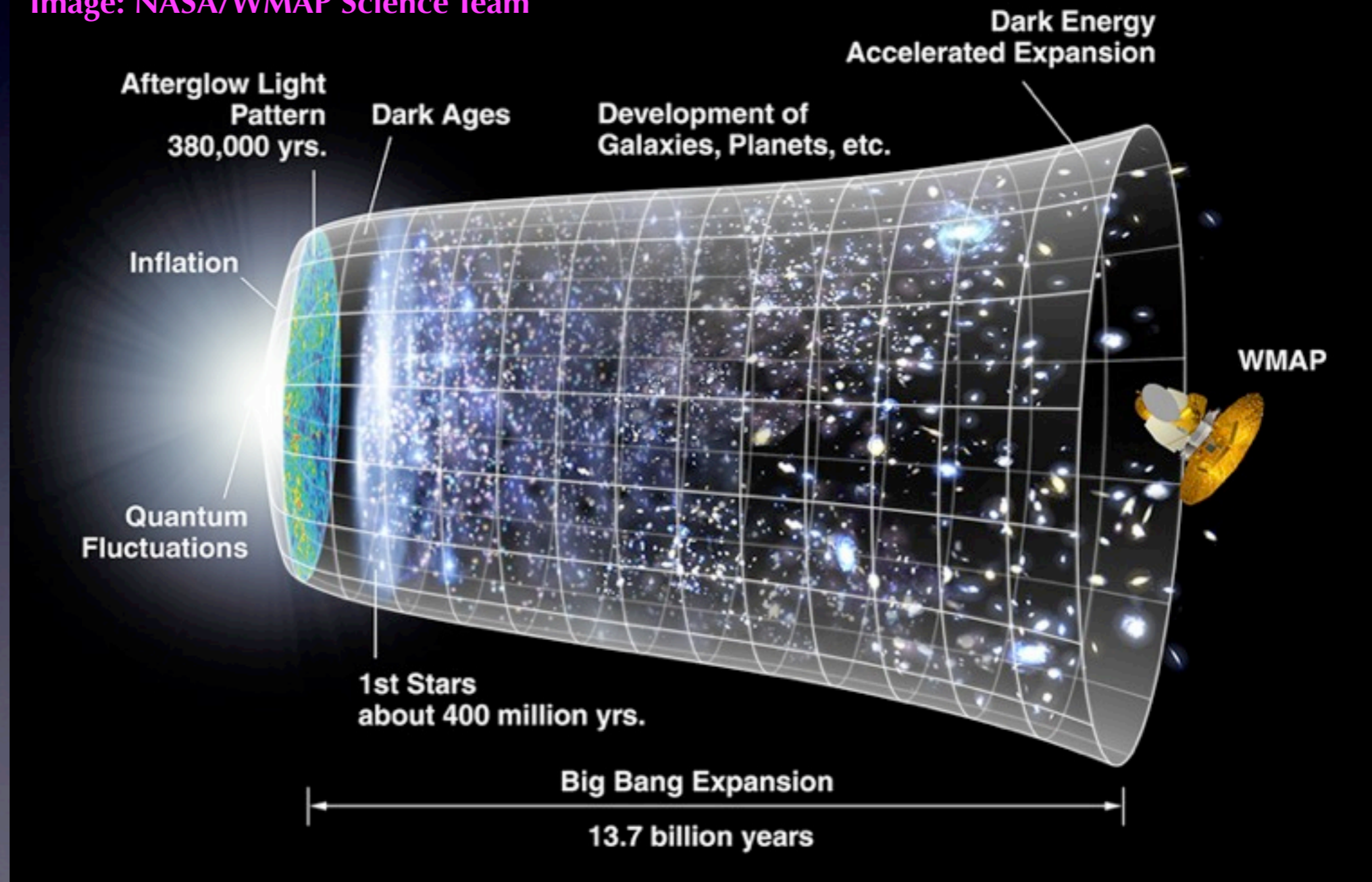
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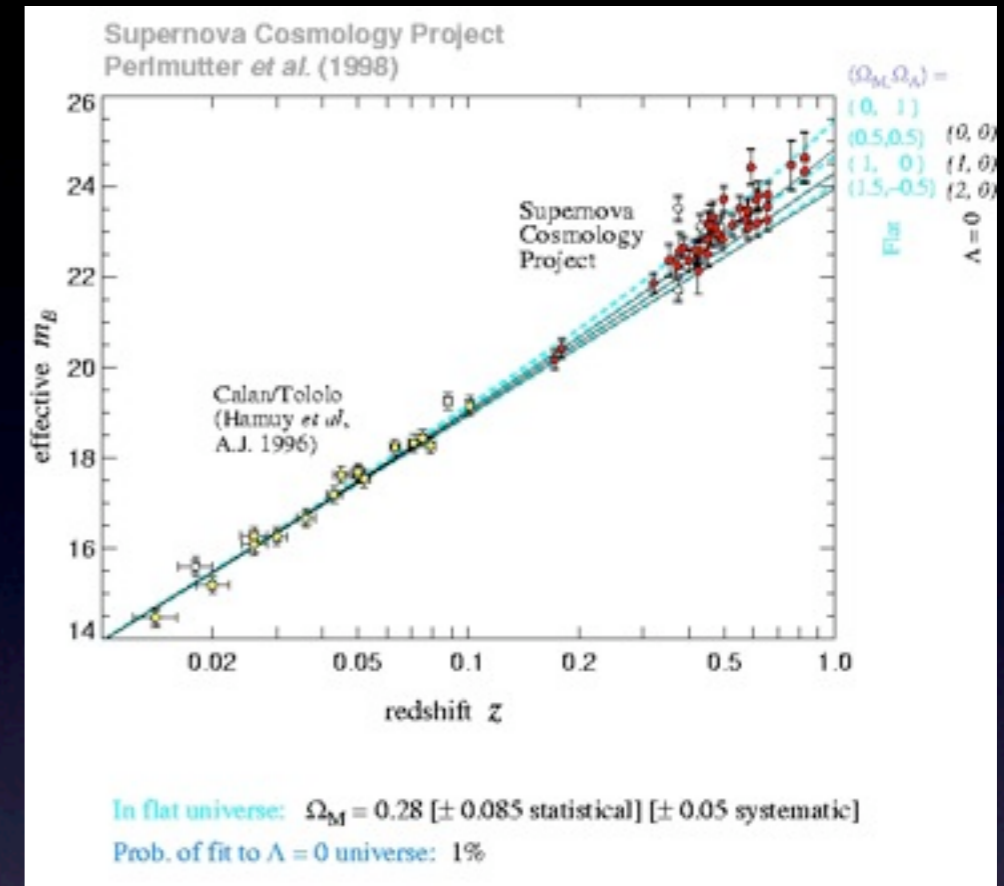
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Lecture plan

- Lecture 1: Cosmology overview
 - Basics of inflationary cosmology
- Lecture 2: Observational status of inflation
- Lecture 3: The inflation-building toolkit.

Cosmological overview



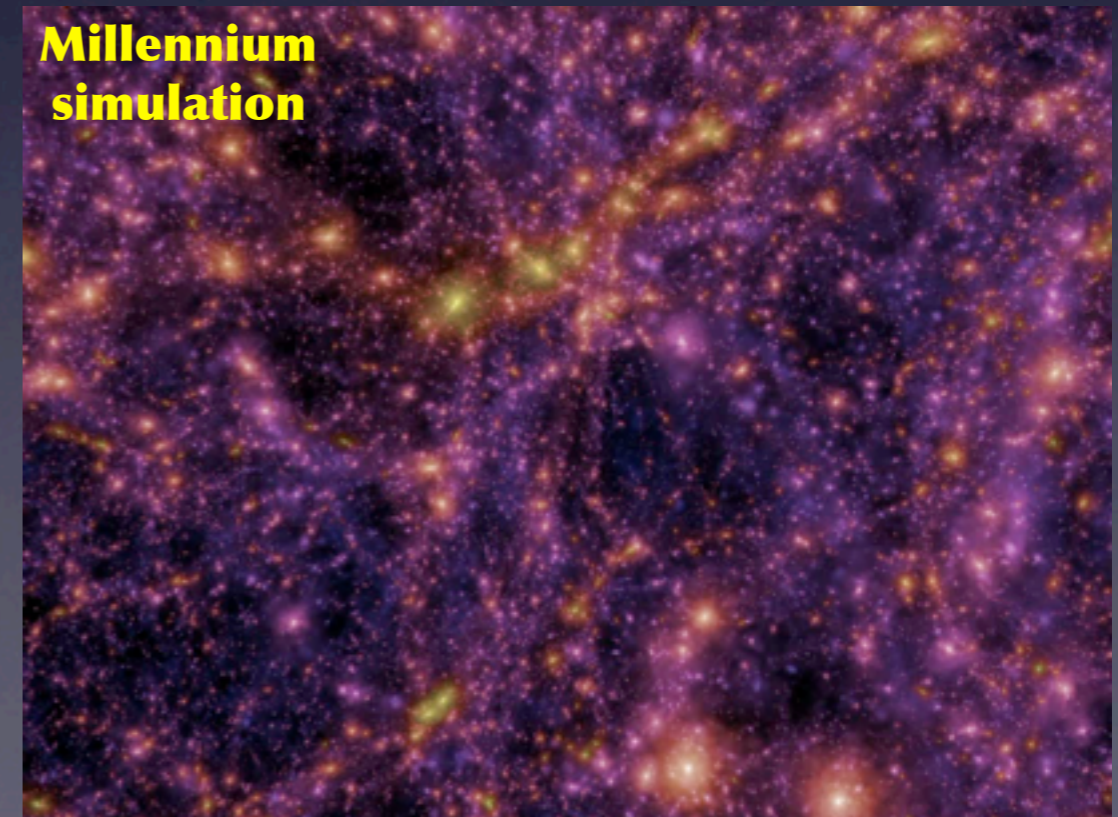
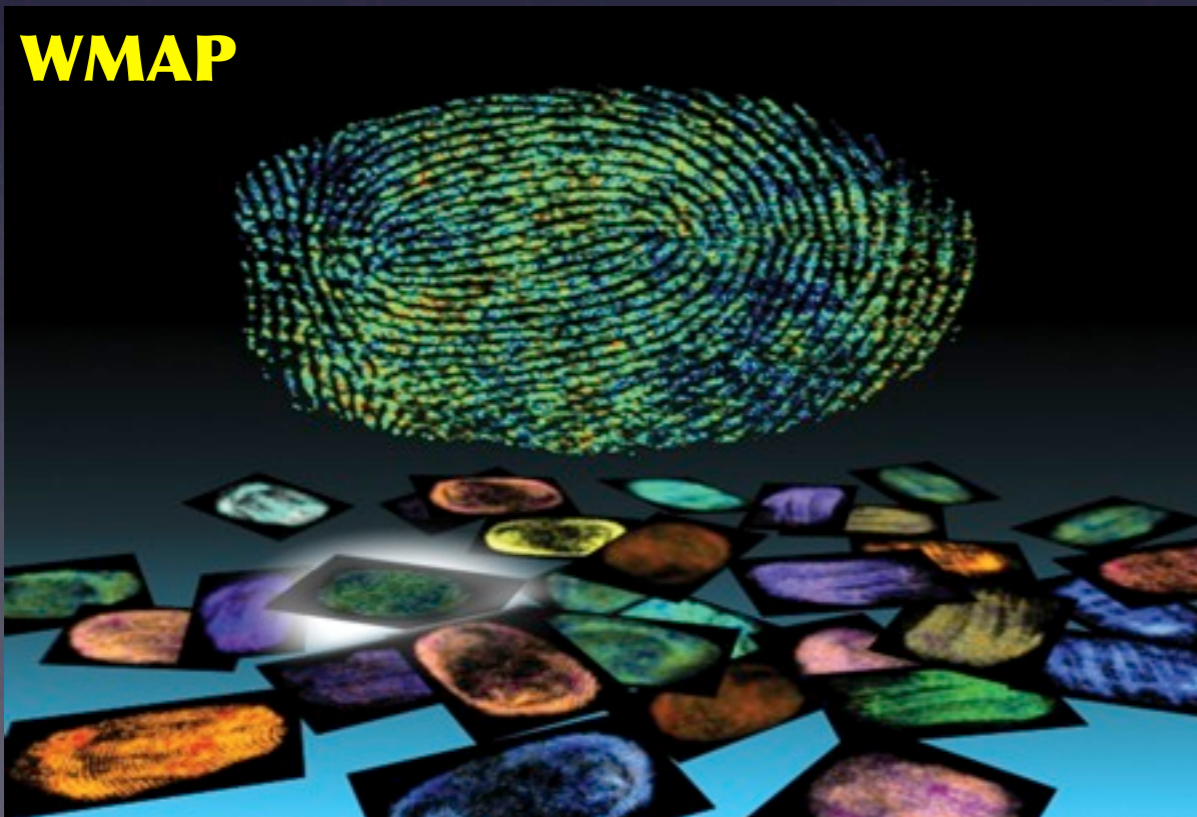
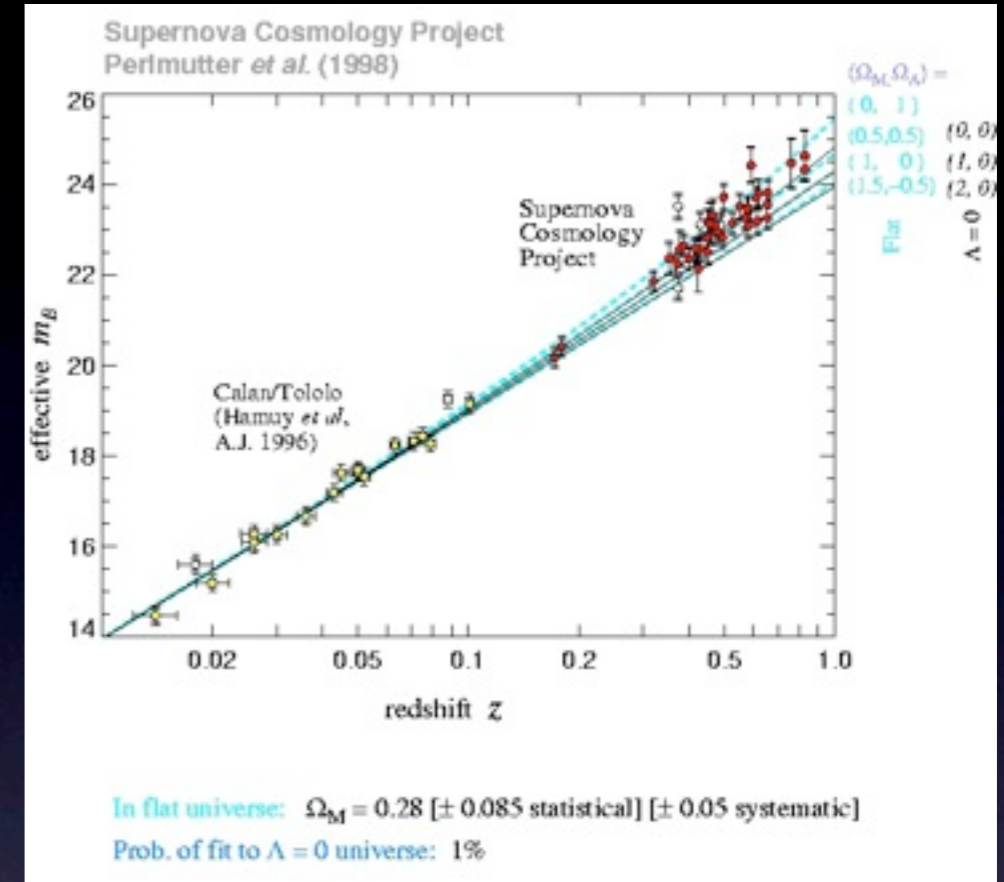
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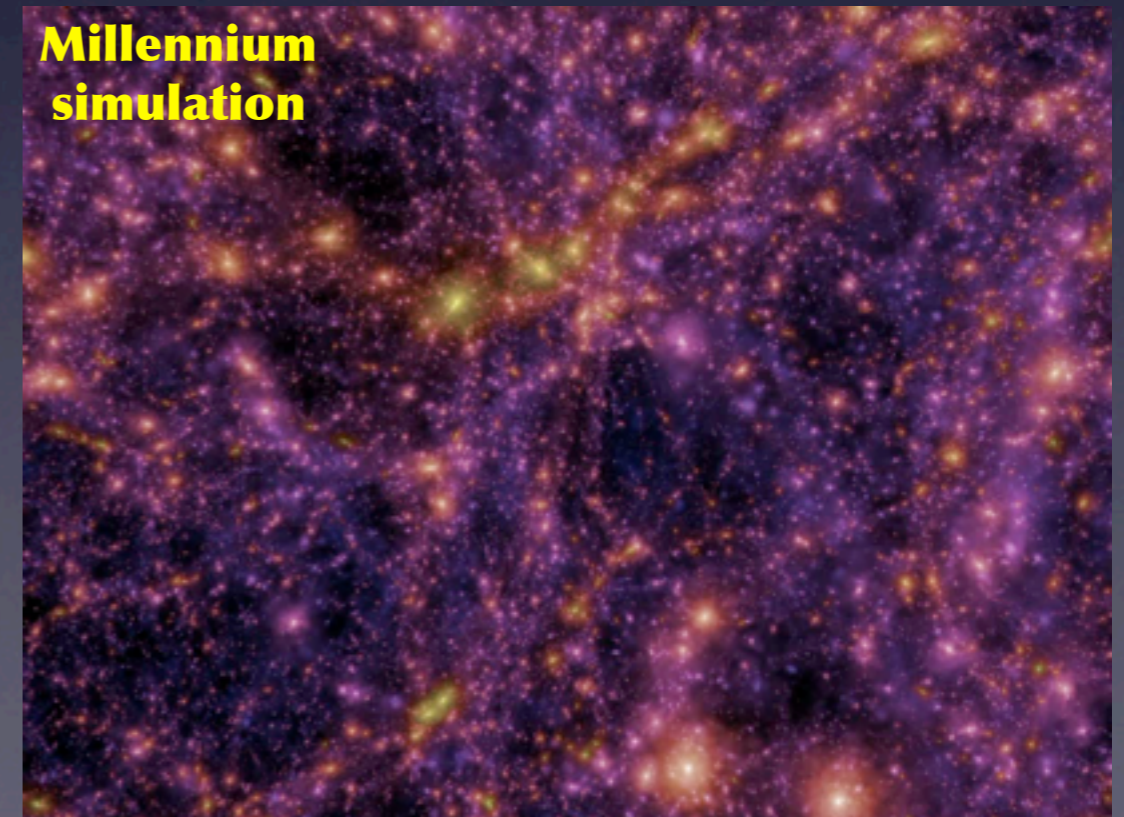
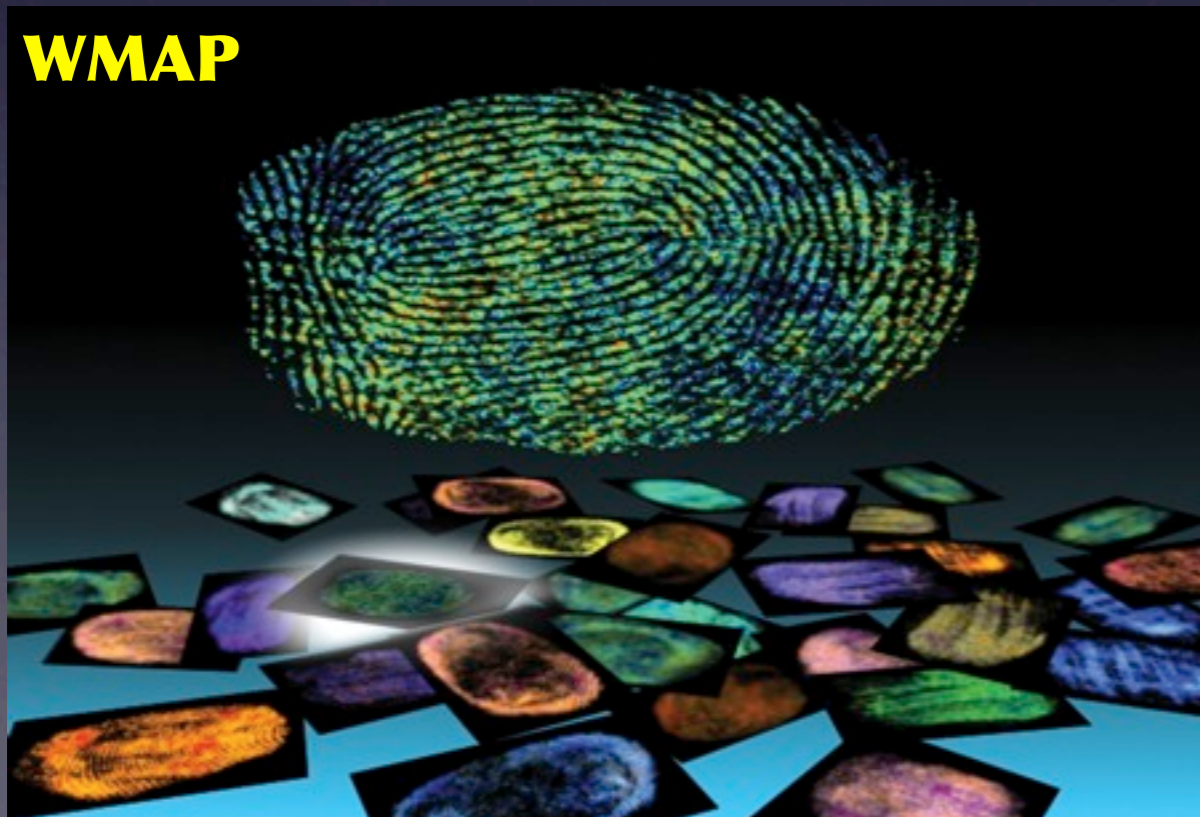
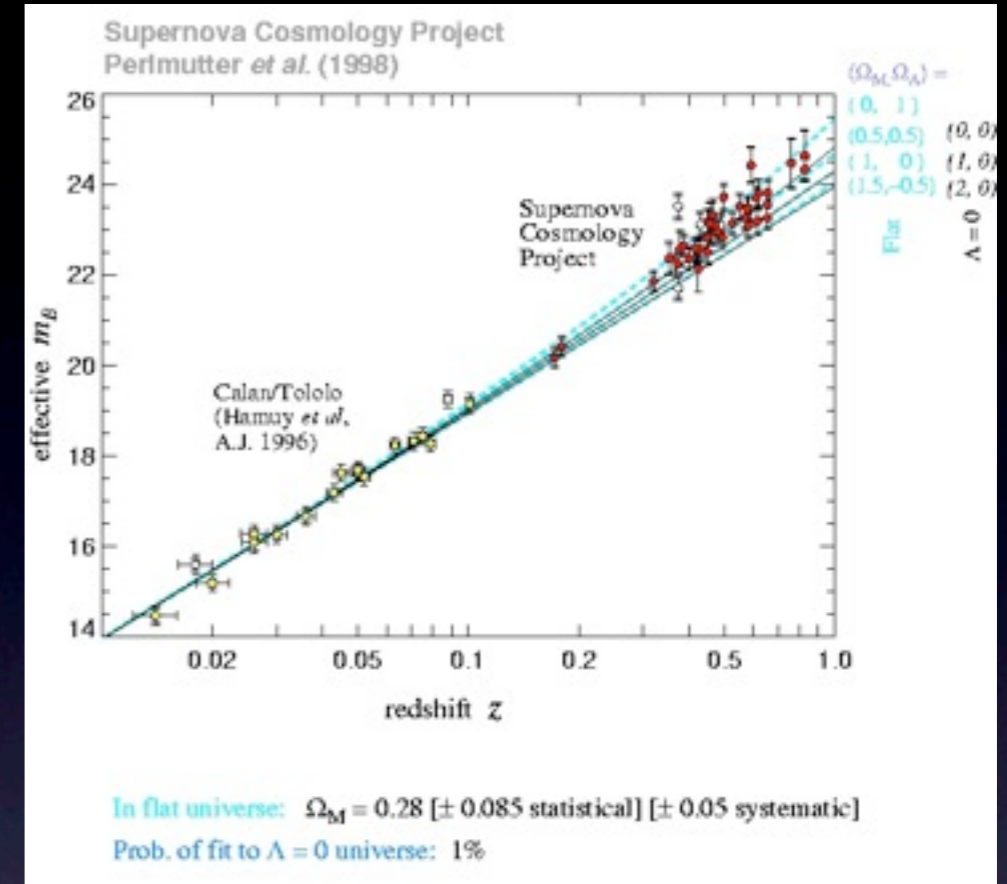
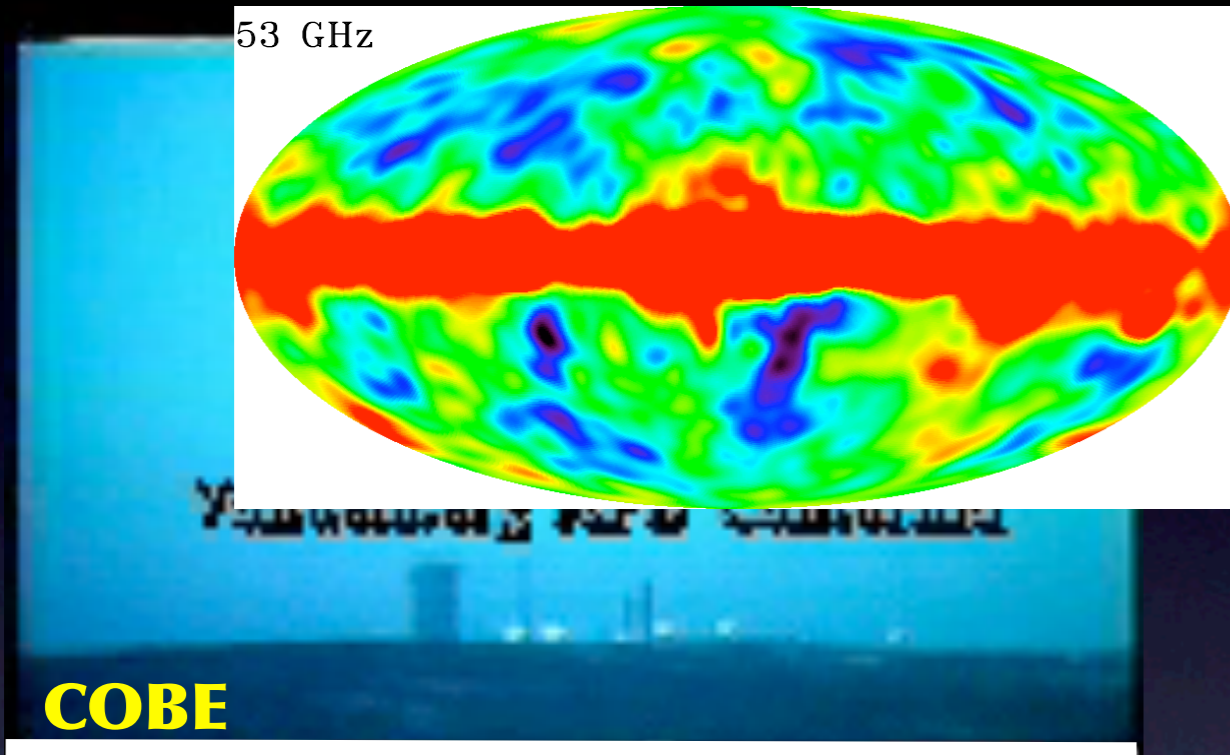


**Millennium
simulation**

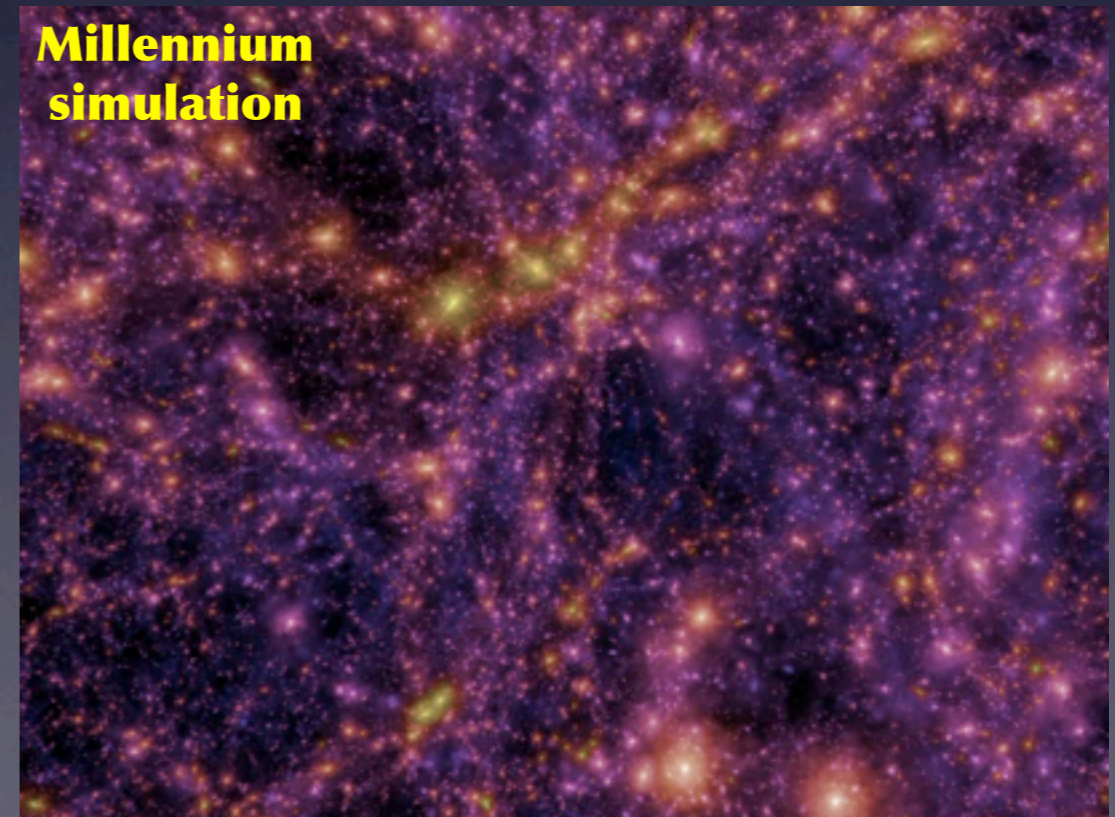
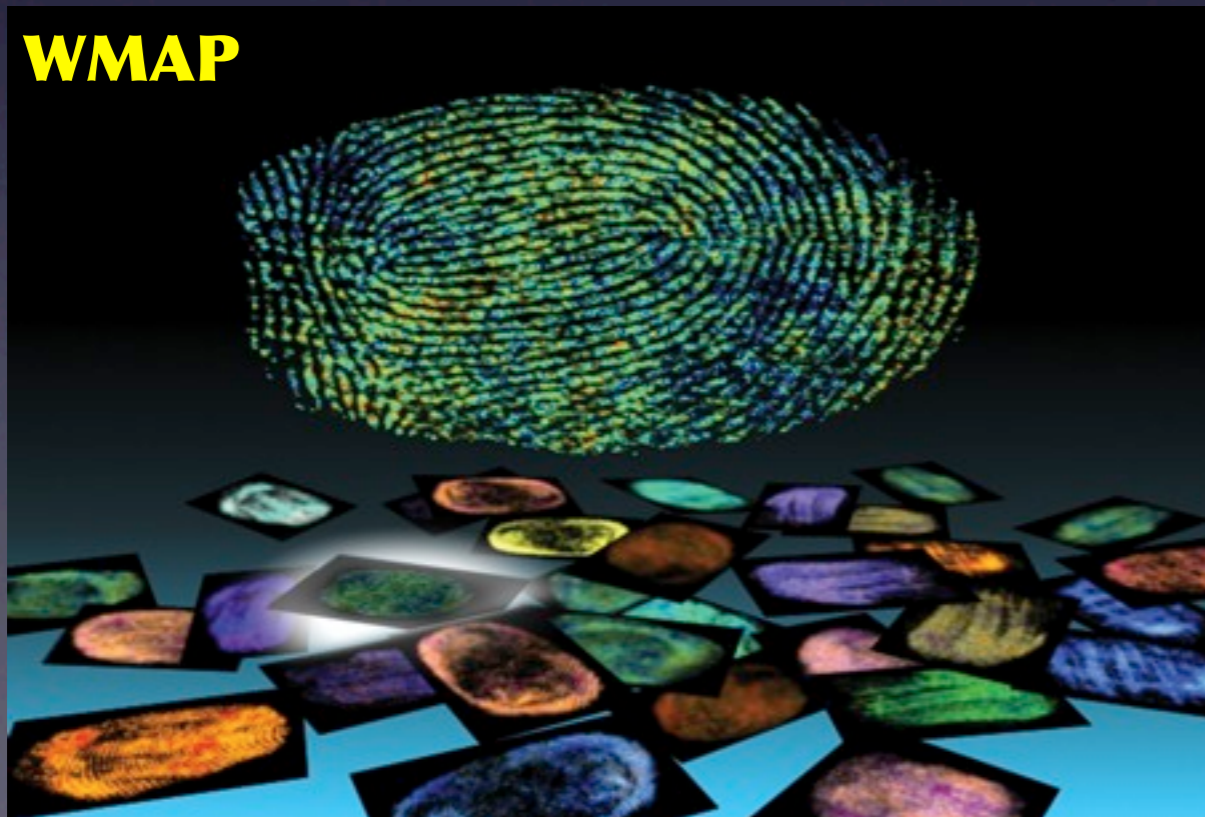
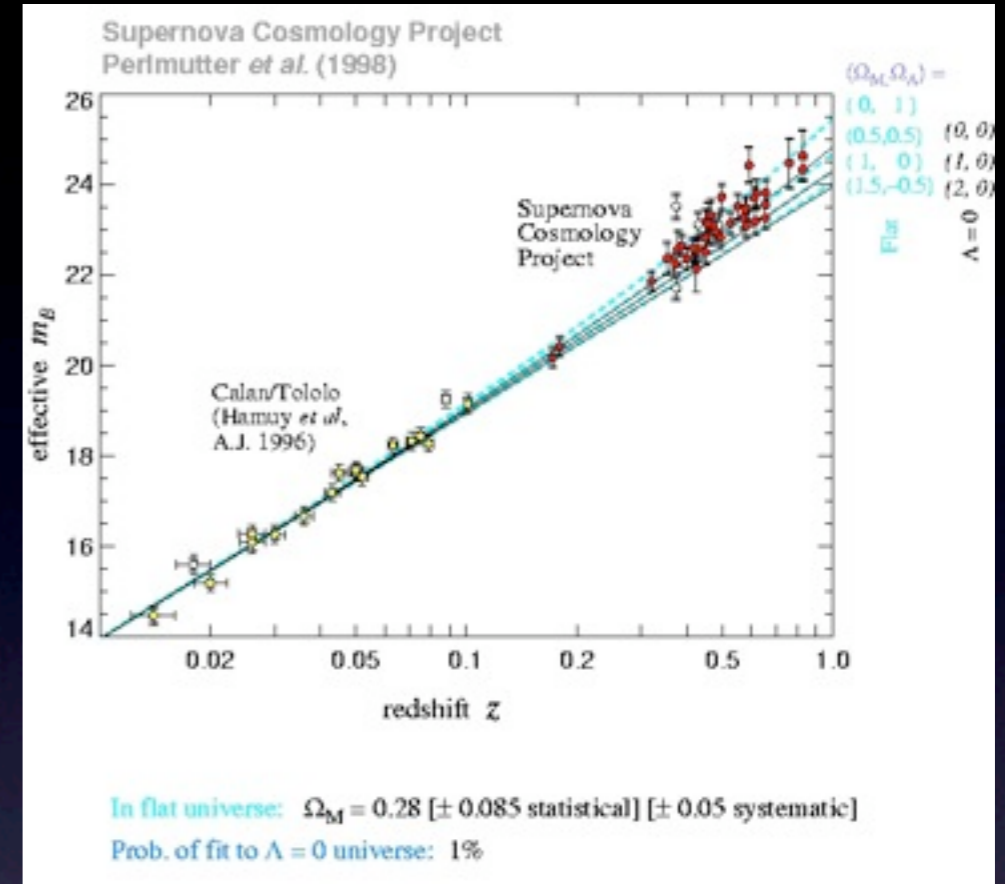
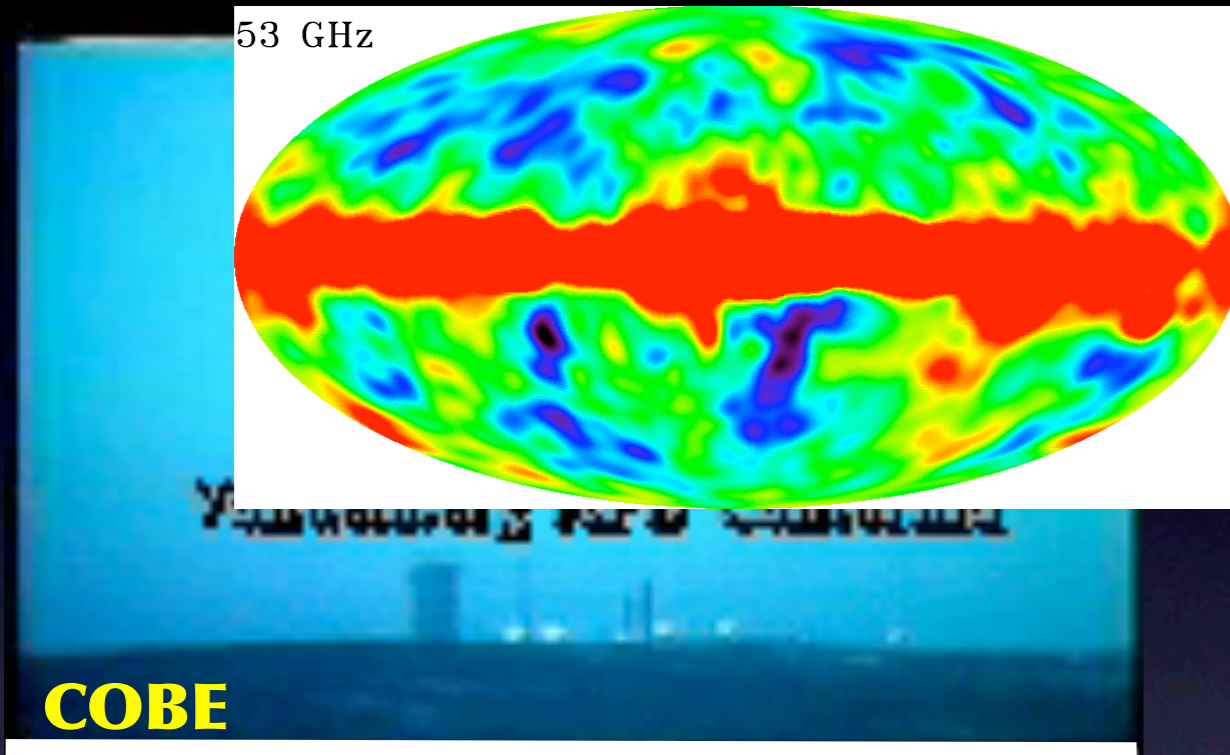
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■ Inflationary cosmology

The leading candidate theory for explaining where those initial irregularities came from: quantum fluctuations during rapid expansion of the young Universe.

What cosmological parameters?

The standard assumption is that the present Universe contains five types of material.

- Baryons (ie protons, neutrons and electrons)
- Radiation (photons)
- Neutrinos
- Dark matter
- Dark energy (eg cosmological constant)

The sum of their densities, plus the expansion rate, determines the spatial curvature, which nowadays is usually assumed to vanish.

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Plus the theoretical technology necessary to develop observational predictions based on the model assumptions.

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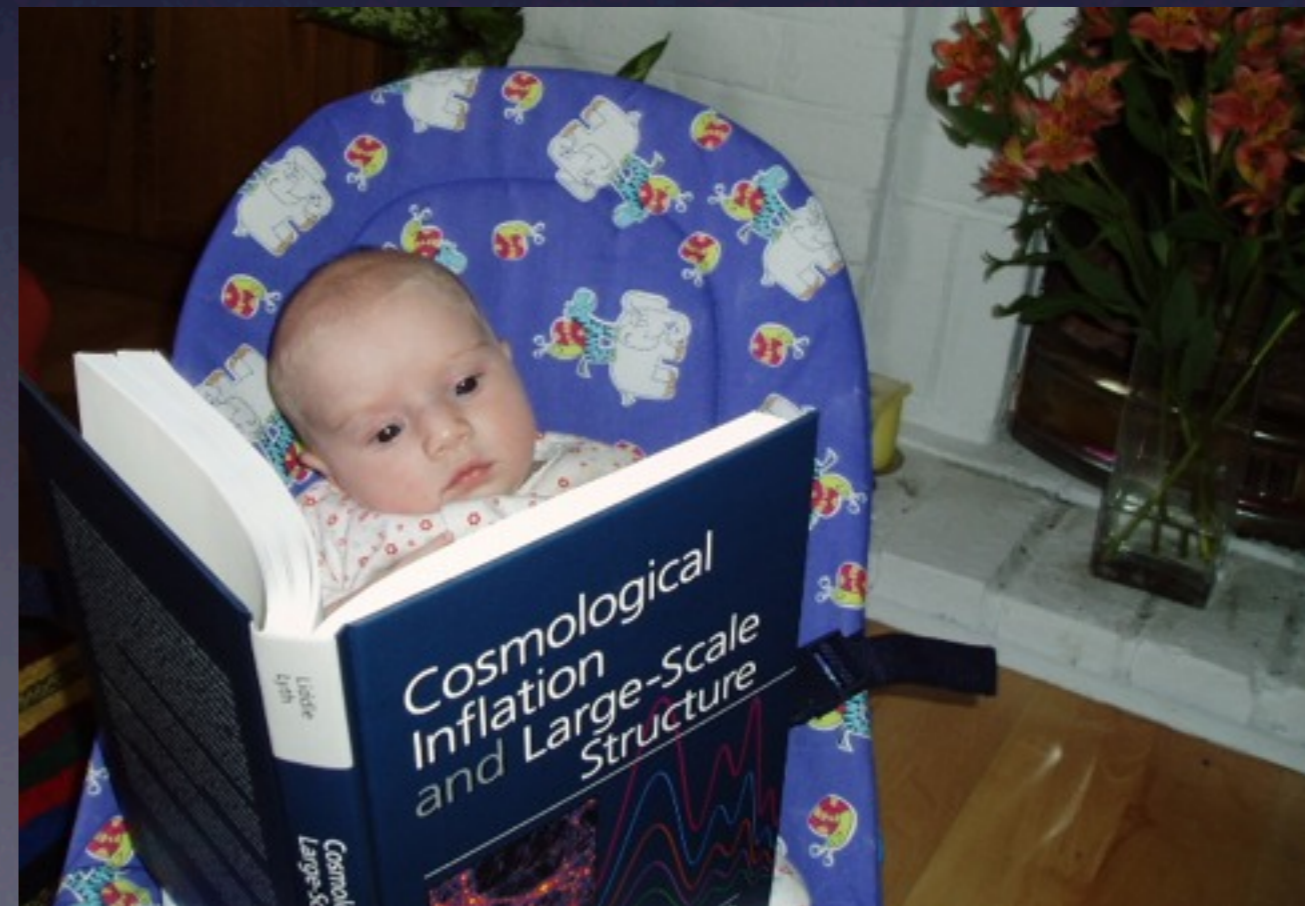
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- Can fundamental properties of the Universe be predicted by theory at all?

Lecture 1

The basics of inflationary cosmology



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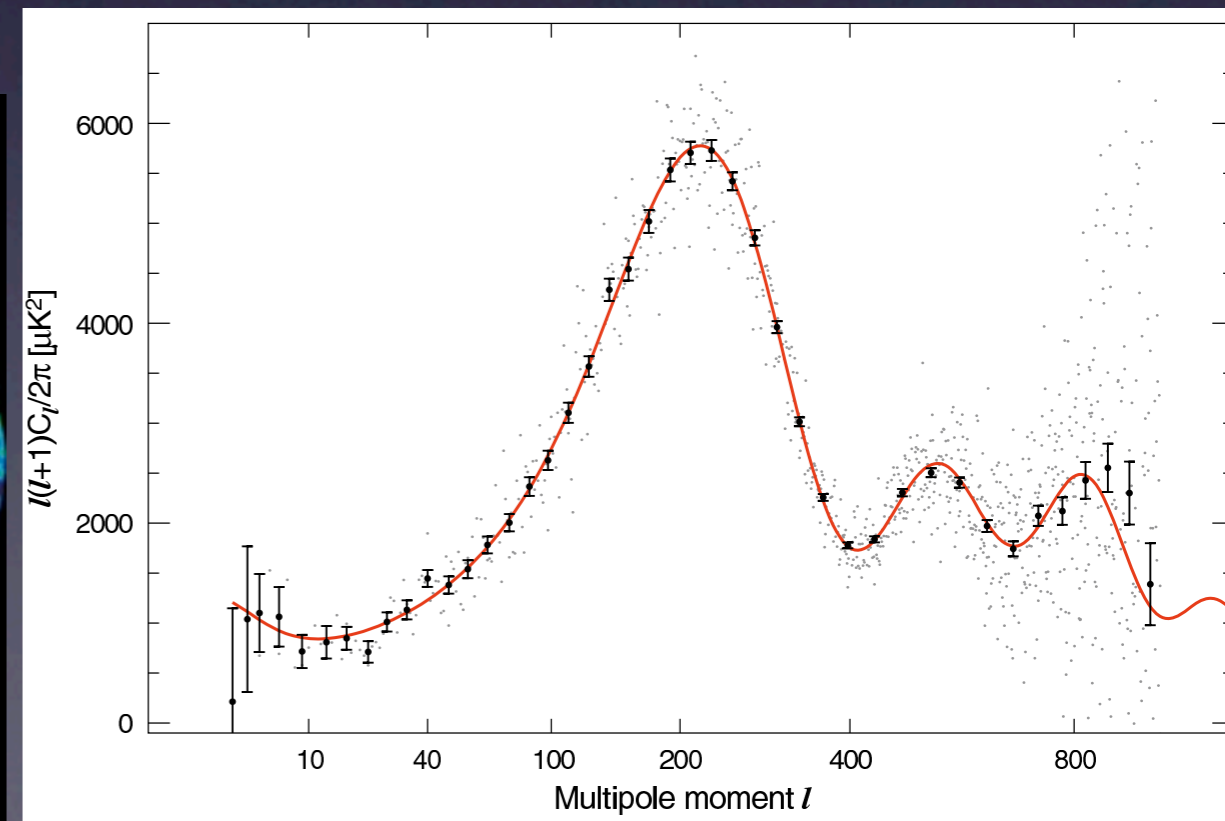
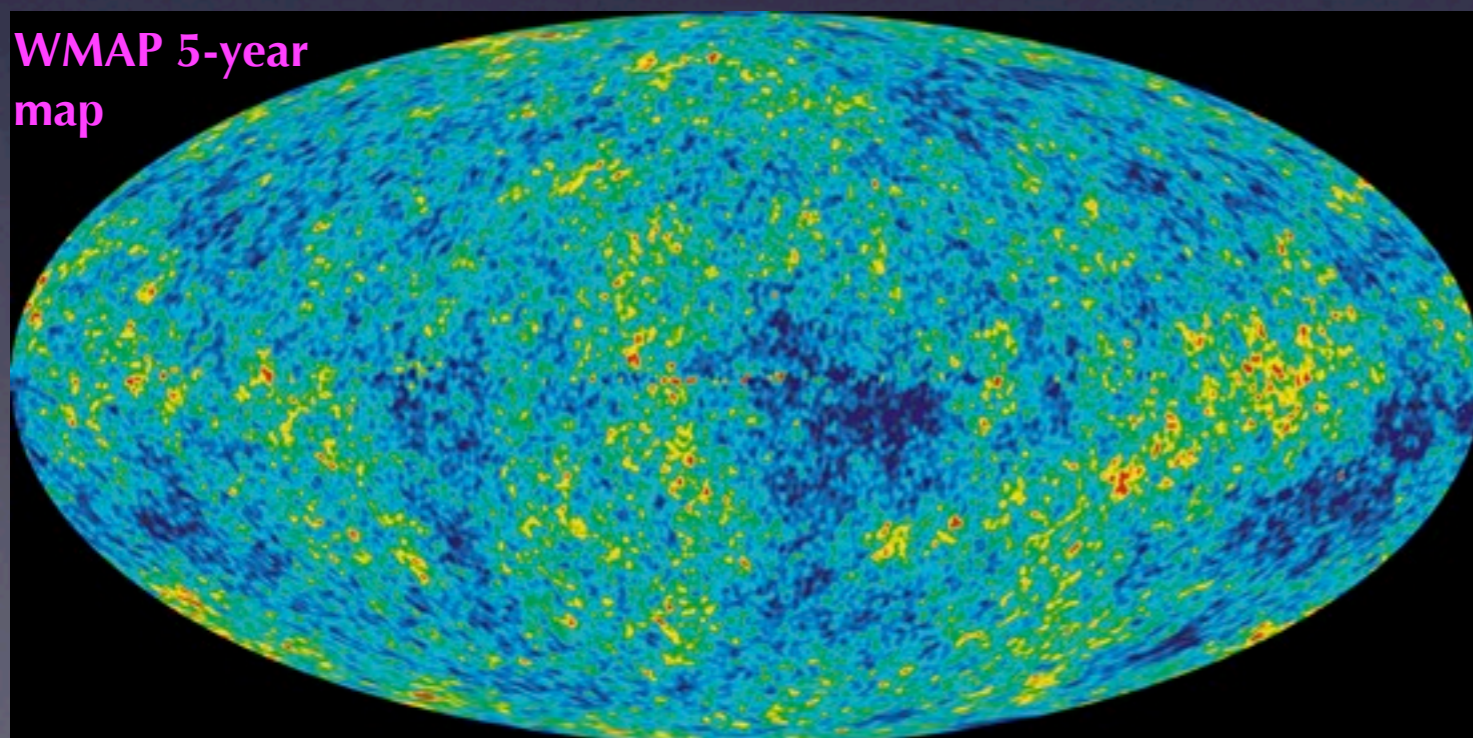
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and so acceleration requires $p < -\rho c^2/3$

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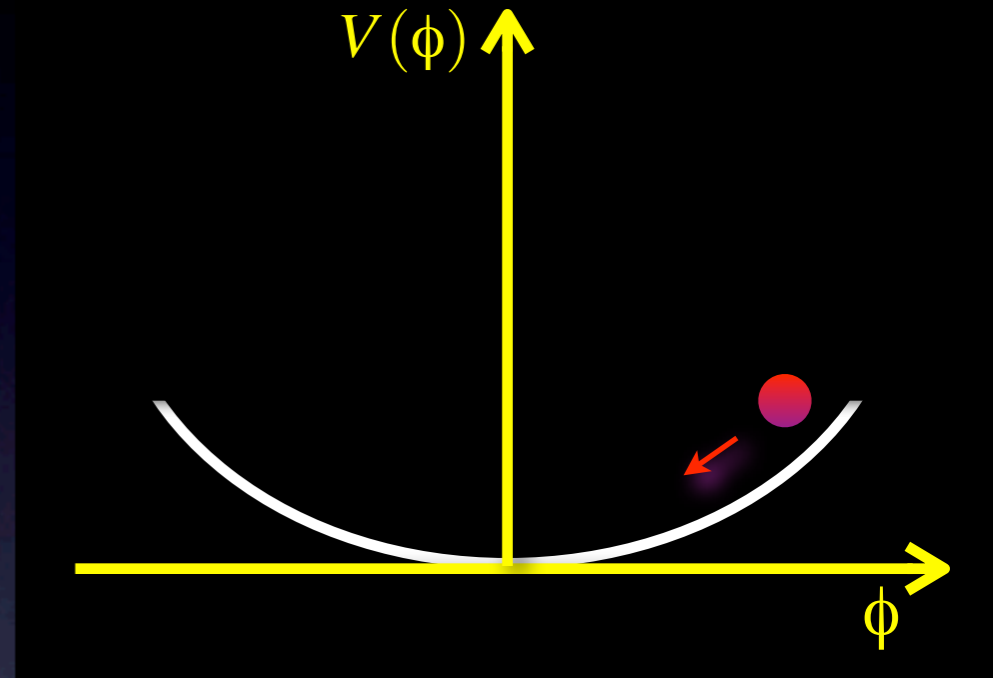
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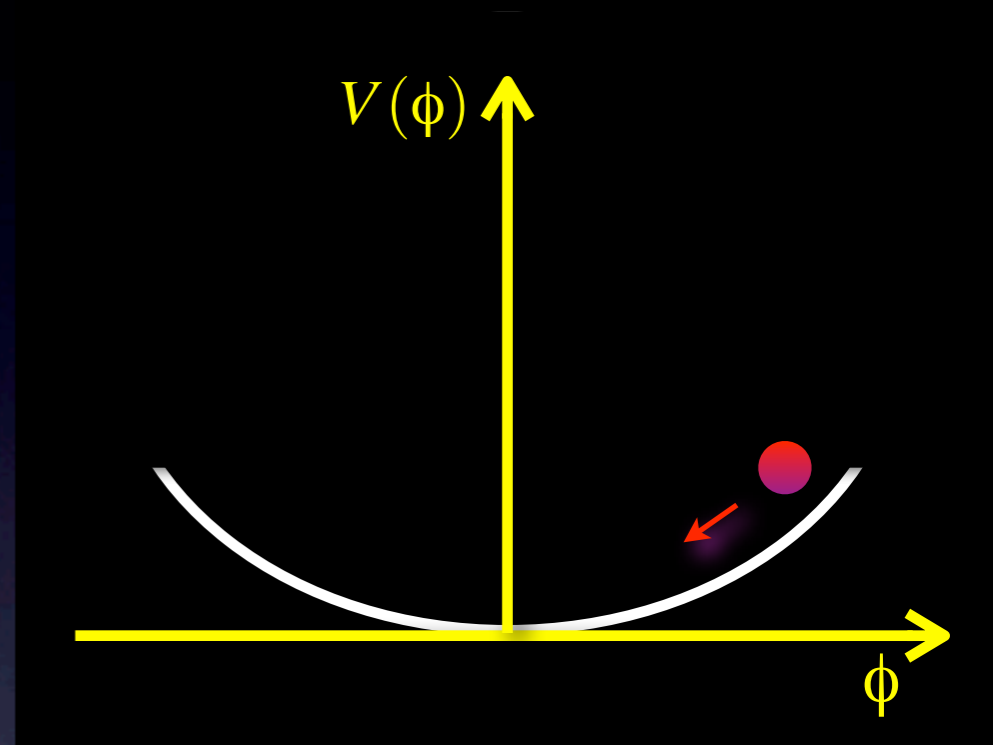
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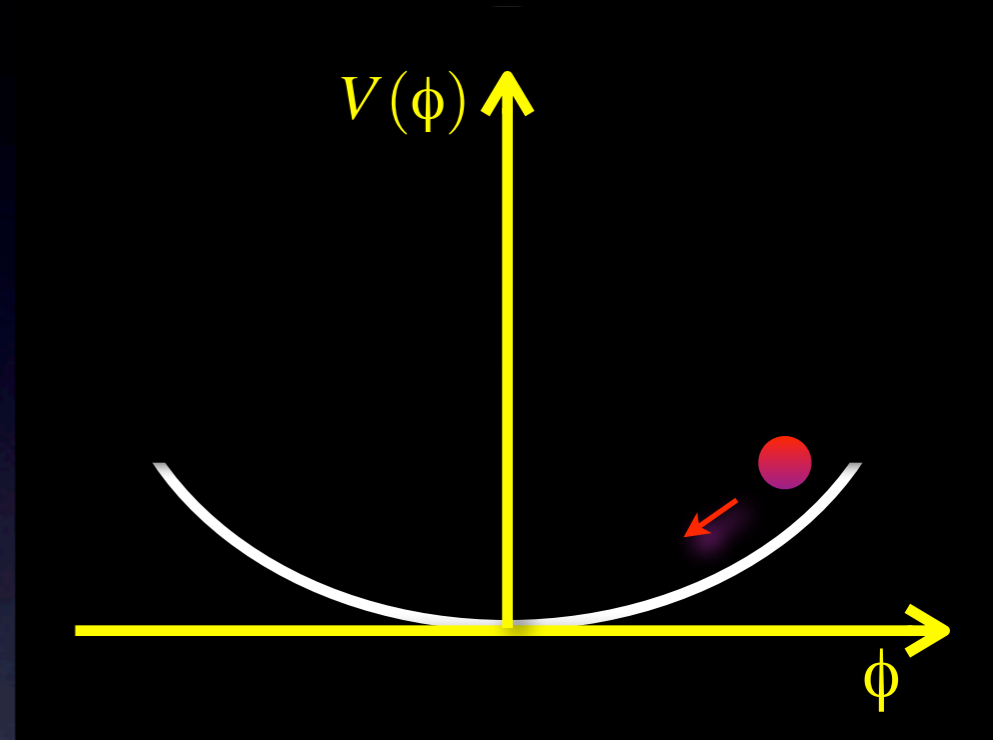
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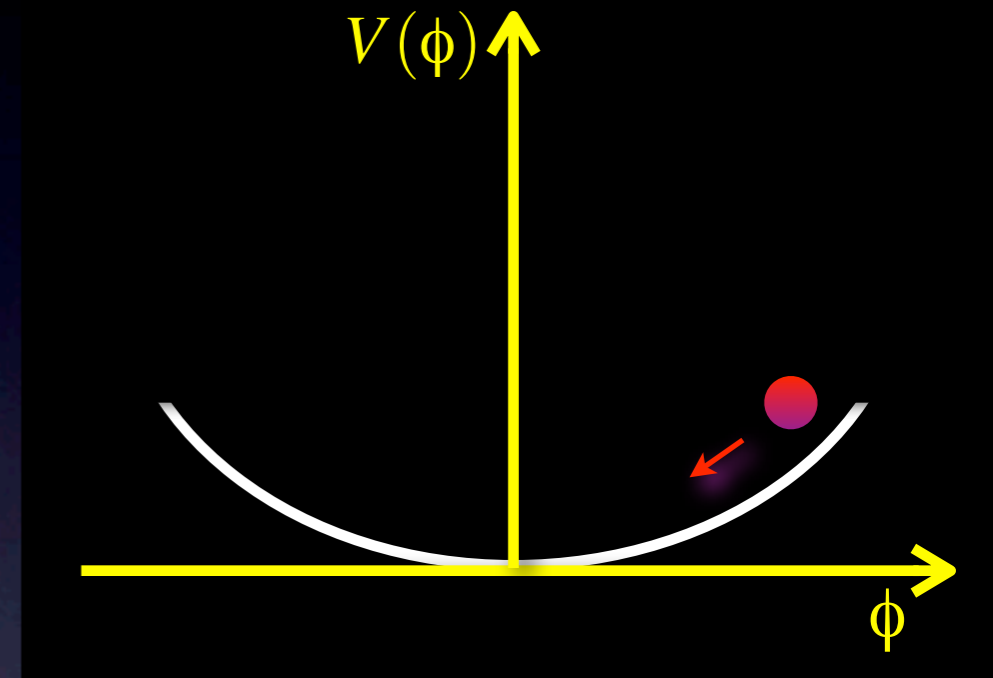
For now I will assume there is just a single field, though many models have more.



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The scalar field potential

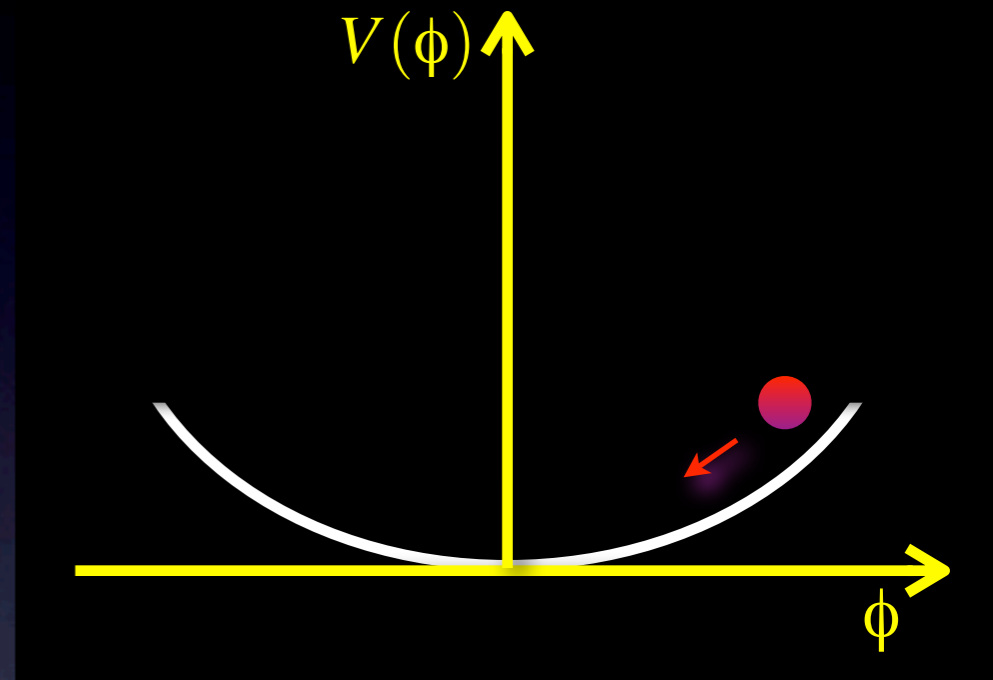
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Unfortunately no fundamental scalar field has ever been observed, though particle theories predicts large numbers of them. In cosmology, we aim to constrain the potential using observations.

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Inflation and perturbations

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- Scalar field fluctuations
 - Lead to scalar metric perturbations
 - Cause gravitational collapse to form structures
- Gravitational wave perturbations
 - Not associated with gravitational collapse but may influence the CMB.



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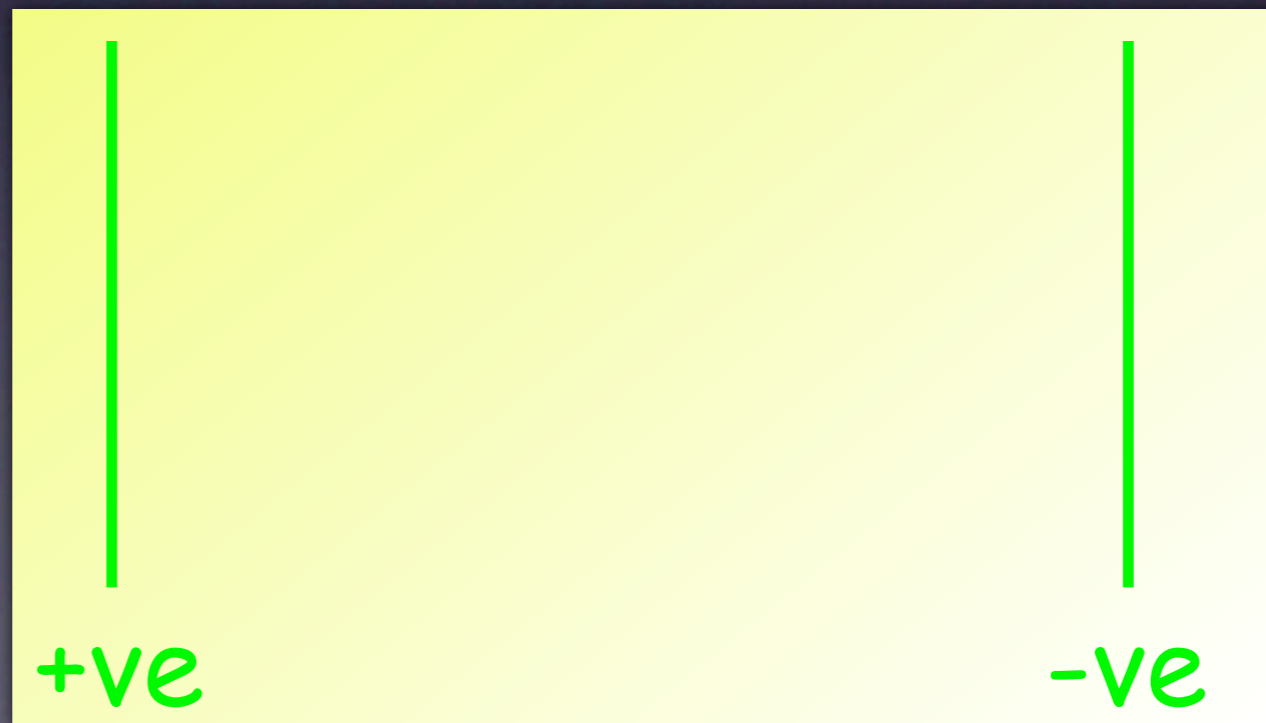
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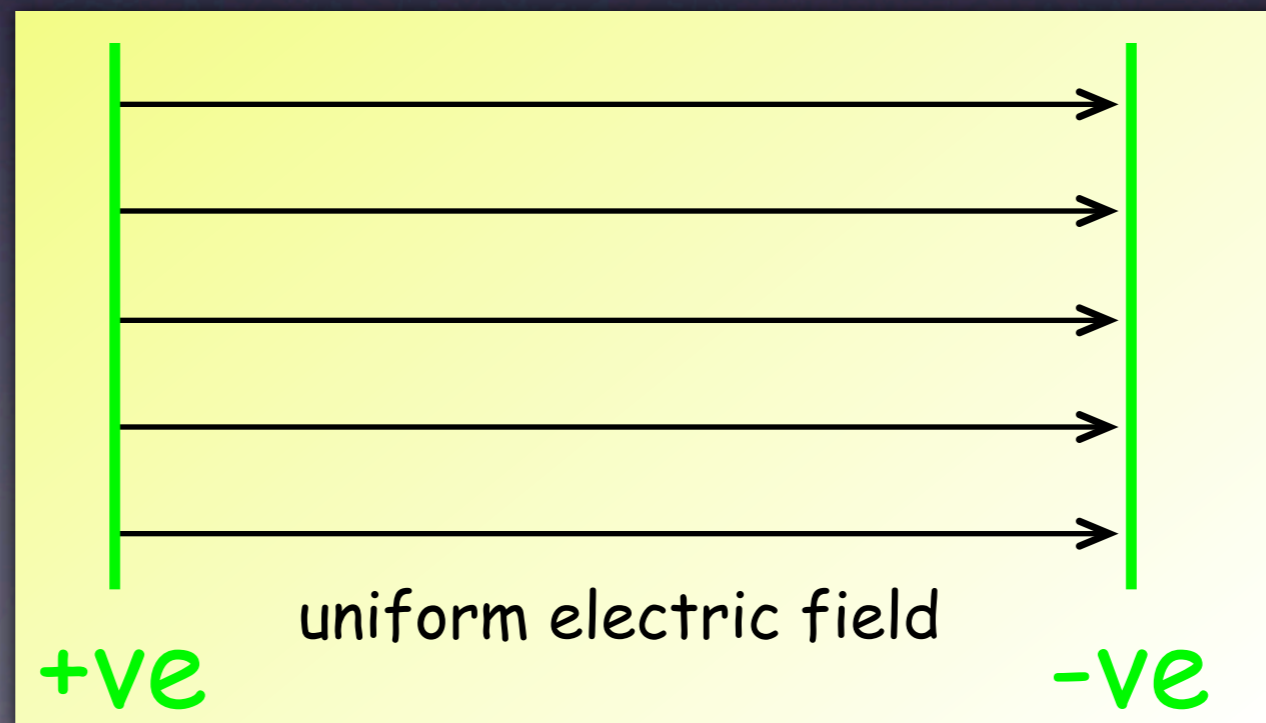


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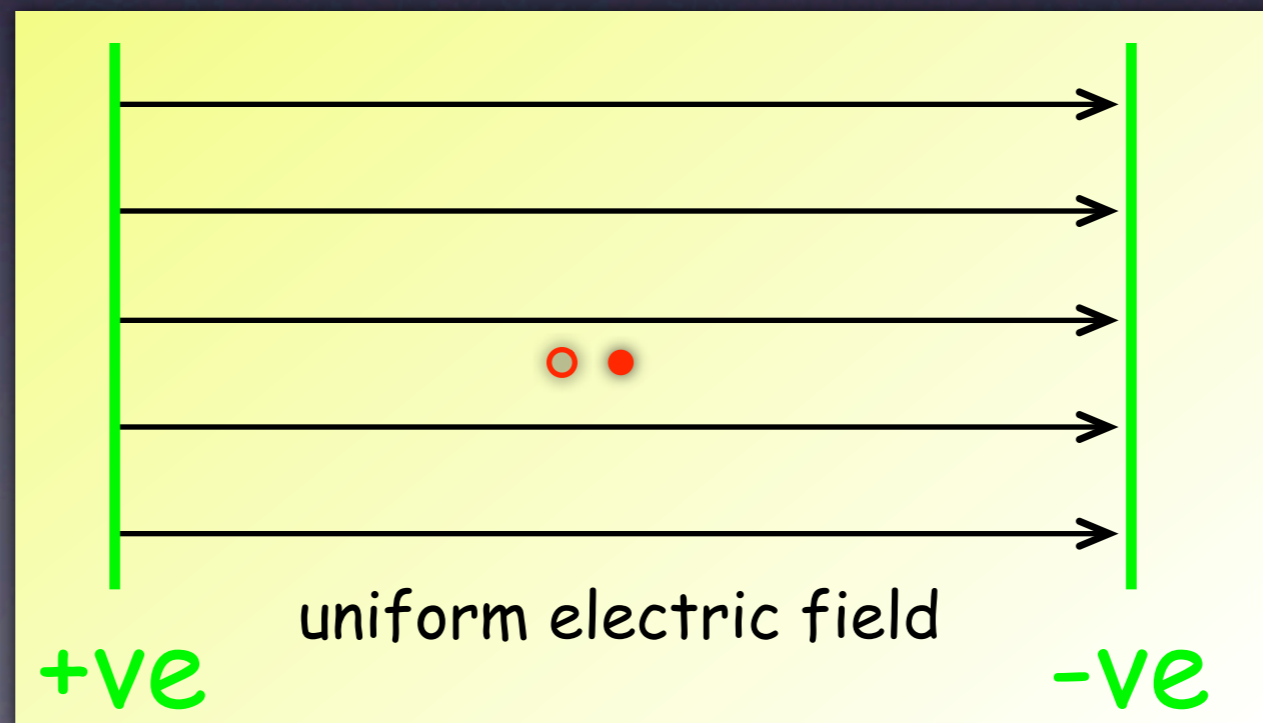


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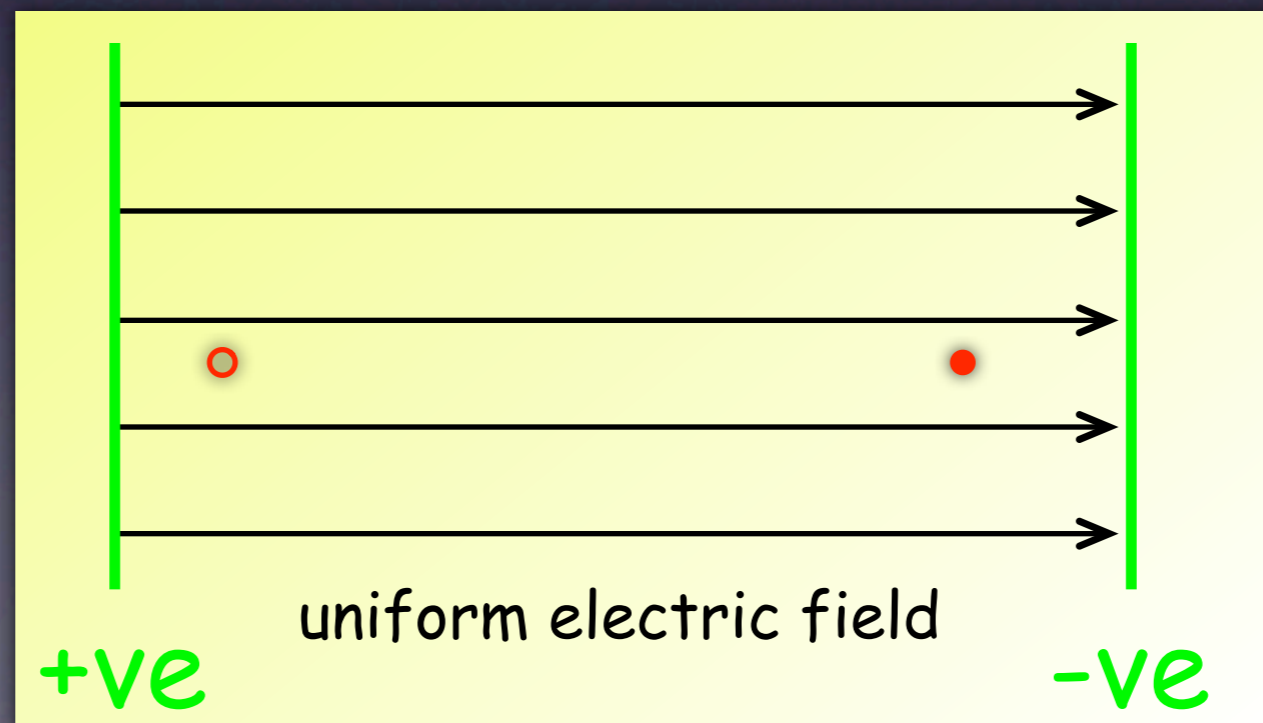
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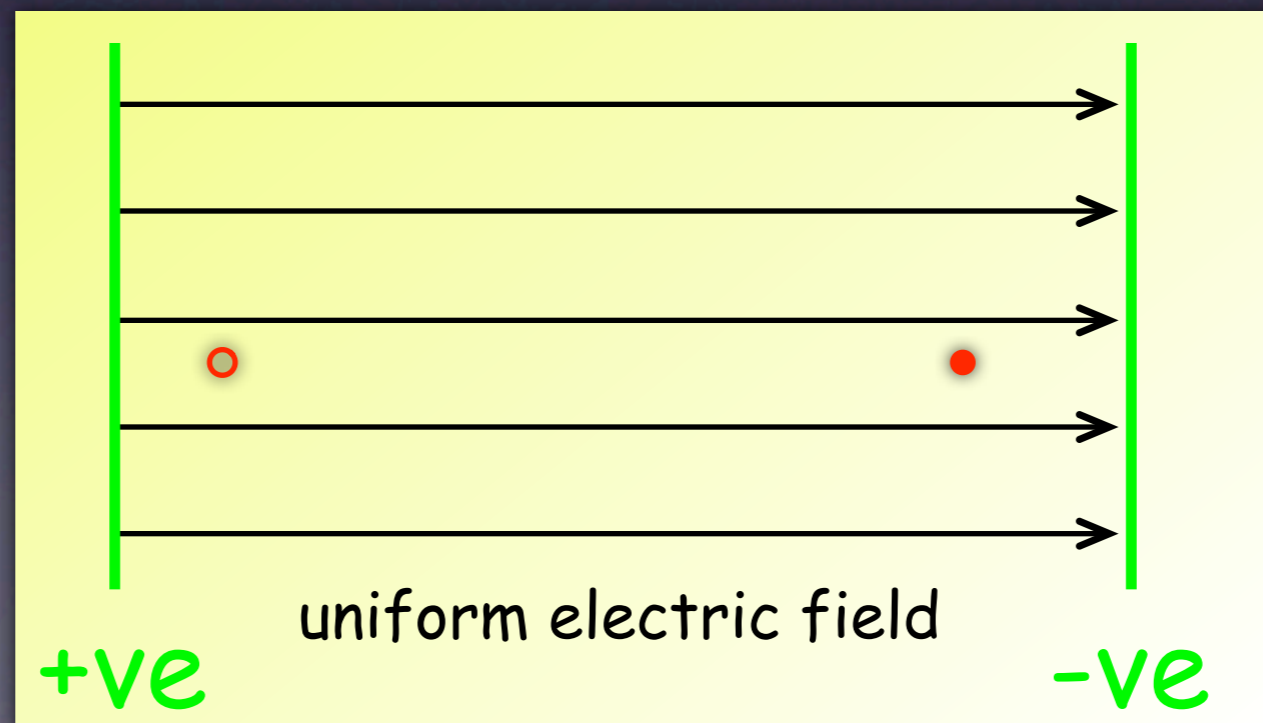
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The pair production breaks the initial homogeneity.



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Gravitational waves

$$r = 16\varepsilon \quad n_G = -2\varepsilon = -\frac{r}{8}$$

Other inflationary perturbations

It is a very reasonable working hypothesis that the single-field paradigm holds, and much work goes into constraining inflationary models of this type. But there is a broader phenomenology:

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- **Inhomogeneous reheating:** Auxiliary field modulates the decay of the inflaton into conventional material.

