# Appendix C <br> Vertices in 4D-OPP's defined in terms of Manifold and Non-Manifold Edges and Their Corresponding 4D Configurations 

We will describe and classify these vertices in 4D-OPP's depending on the number of Manifold and Non-Manifold edges incident to them. In the nomenclature to use "V" means vertex, the first digit shows the number of incident Manifold edges, the " N " followed by a digit is present if there are incident Non-Manifold edges to the vertex and the digit indicates the number of such edges, and a third digit is included to distinguish between two different types that otherwise could receive the same name. In each vertex continuous lines indicate Manifold edges and dotted lines indicate Non-Manifold edges.

| V0 |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
| Number of <br> surrounding <br> Hyper-boxes | Corresponding <br> Configurations <br> (see Appendix A) | Number of <br> surrounding <br> Hyper-boxes | Corresponding <br> Configurations <br> (see Appendix A) |  |
| 0 | 1 | 16 | 253 |  |
| 4 | 13 | 12 | 241 |  |
| 8 | 109 |  |  |  |
| 132 |  |  |  |  |

V0N2

| Number of <br> surrounding <br> Hyper-boxes | Corresponding <br> Configurations <br> (see Appendix A) | Number of <br> surrounding <br> Hyper-boxes | Corresponding <br> Configurations <br> (see Appendix A) |  |
| :---: | :---: | :---: | :---: | :---: |
| 4 | 17 | 12 | 231 |  |
| 6 | 26 | 10 | 198 |  |
| 8 | 62 |  |  |  |
| 6 | 120 |  |  |  |


| V0N5 |  |  |  |
| :---: | :---: | :---: | :---: |
| Number of surrounding Hyper-boxes | Corresponding Configurations (see Appendix A) | Number of surrounding Hyper-boxes | $\begin{gathered} \text { Corresponding } \\ \text { Configurations } \\ \text { (see Appendix A) } \\ \hline \end{gathered}$ |
| 7 | 105 | 9 | 147 |
|  |  |  |  |
| Number of surrounding Hyper-boxes | $\begin{gathered} \hline \text { Corresponding } \\ \text { Configurations } \\ \text { (see Appendix A) } \end{gathered}$ | Number of surrounding Hyper-boxes | $\begin{gathered} \hline \text { Corresponding } \\ \text { Configurations } \\ \text { (see Appendix A) } \end{gathered}$ |
| 5 | 42 | 10 | 197 |
| 8 | $\begin{aligned} & \hline 141 \\ & 143 \\ & \hline \end{aligned}$ |  |  |

V0N7

| Number of <br> surrounding <br> Hyper-boxes | Corresponding <br> Configurations <br> (see Appendix A) | Number of <br> surrounding <br> Hyper-boxes | Corresponding <br> Configurations <br> (see Appendix A) |  |
| :---: | :---: | :---: | :---: | :---: |
| 4 | 18 | 12 | 230 |  |
| 5 | 43 | 11 | 209 |  |
| 6 | 64 | 10 | 180 |  |
|  | 72 |  | 184 |  |
| 7 | 76 | 9 | 149 |  |
| 8 | 106 |  |  |  |



| V1N4-2 |  |
| :---: | :---: |
| Number of <br> surrounding <br> Hyper-boxes | Corresponding <br> Configurations <br> (see Appendix A) |
| 9 | 156 |


| V1N5 |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
| Number of <br> surrounding <br> Hyper-boxes | Corresponding <br> Configurations <br> (see Appendix A) | Number of <br> surrounding <br> Hyper-boxes | Corresponding <br> Configurations <br> (see Appendix A) |  |
| 4 | 25 | 12 | 232 |  |
| 6 | 65 |  |  |  |
|  |  |  |  |  |



V1N7

| Number of surrounding Hyper-boxes | Corresponding Configurations (see Appendix A) | Number of surrounding Hyper-boxes | Corresponding Configurations (see Appendix A) |
| :---: | :---: | :---: | :---: |
| 4 | 21 | 12 | 228 |
| 5 | $36$ | 11 | $208$ |
| 6 | $\begin{aligned} & 71 \\ & 73 \end{aligned}$ | 10 | $\begin{aligned} & 182 \\ & 183 \\ & 188 \end{aligned}$ |
| 7 | $\begin{gathered} 95 \\ 97 \\ 103 \\ \hline \end{gathered}$ | 9 | $\begin{aligned} & 154 \\ & 157 \end{aligned}$ |
| 8 | $\begin{aligned} & 133 \\ & 135 \\ & 137 \end{aligned}$ |  |  |


|  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
| Number of <br> surrounding <br> Hyper-boxes | Corresponding <br> Configurations <br> (see Appendix A) | Number of <br> surrounding <br> Hyper-boxes | Corresponding <br> Configurations <br> (see Appendix A) |  |
| 2 | 3 | 14 | 251 |  |
| 6 | 49 | 10 | 205 |  |
| 8 | 116 |  |  |  |


|  |  |
| :---: | :---: |
| Number of <br> surrounding <br> Hyper-boxes | Corresponding <br> Configurations <br> (see Appendix A) |
| 4 |  |



V2N2-2

| Number of <br> surrounding <br> Hyper-boxes | Corresponding <br> Configurations <br> (see Appendix A) |
| :---: | :---: |
| 9 | 163 |
| 11 | 224 |



| Number of <br> surrounding <br> Hyper-boxes | Corresponding <br> Configurations <br> (see Appendix A) | Number of <br> surrounding <br> Hyper-boxes | Corresponding <br> Configurations <br> (see Appendix A) |
| :---: | :---: | :---: | :---: |
| 4 | 16 | 12 | 238 |
| 8 | 113 |  |  |
|  | 131 |  |  |



V2N3-2

| Number of <br> surrounding <br> Hyper-boxes | Corresponding <br> Configurations <br> (see Appendix A) | Number of <br> surrounding <br> Hyper-boxes | Corresponding <br> Configurations <br> (see Appendix A) |  |
| :---: | :---: | :---: | :---: | :---: |
| 5 | 44 | 11 | 212 |  |
| 7 | 89 |  |  |  |

## V2N3-3

| Number of <br> surrounding <br> Hyper-boxes | Corresponding <br> Configurations <br> (see Appendix A) |
| :---: | :---: |
| 6 | 63 |



V2N3-4

| Number of <br> surrounding <br> Hyper-boxes | Corresponding <br> Configurations <br> (see Appendix A) |
| :---: | :---: |
| 9 | 172 |



| Number of <br> surrounding <br> Hyper-boxes | Corresponding <br> Configurations <br> (see Appendix A) | Number of <br> surrounding <br> Hyper-boxes | Corresponding <br> Configurations <br> (see Appendix A) |
| :---: | :---: | :---: | :---: |
| 5 | 33 | 11 | 217 |
| 6 | 53 |  |  |
| 7 | 87 |  |  |
| 7 | 98 |  |  |
| 8 | 119 |  |  |


V2N4-3

| Number of <br> surrounding <br> Hyper-boxes | Corresponding <br> Configurations <br> (see Appendix A) |
| :---: | :---: |
| 8 | 136 |

V2N4-4

| Number of <br> surrounding <br> Hyper-boxes | Corresponding <br> Configurations <br> (see Appendix A) |
| :---: | :---: |
| 8 | 142 |



V2N6

| Number of surrounding Hyper-boxes | Corresponding Configurations (see Appendix A) | Number of surrounding Hyper-boxes | Corresponding Configurations (see Appendix A) |
| :---: | :---: | :---: | :---: |
| 4 | 23 | 12 | 229 |
| 5 | 46 | 11 | 213 |
|  |  |  | 214 |
|  |  |  | 216 |
| 6 | 69 | 10 | 187 |
|  |  |  | 190 |
| 7 | 94 | 9 | 151 |
|  | 96 |  | 159 |
|  |  |  | 161 |
|  |  |  | 162 |
| 8 | 130 |  |  |



| Number of <br> surrounding <br> Hyper-boxes | Corresponding <br> Configurations <br> (see Appendix A) |
| :---: | :---: |
| 5 | 40 |



| Number of <br> surrounding <br> Hyper-boxes | Corresponding <br> Configurations <br> (see Appendix A) | Number of <br> surrounding <br> Hyper-boxes | Corresponding <br> Configurations <br> (see Appendix A) |
| :---: | :---: | :---: | :---: |
| 6 | 68 | 10 | 186 |
| 8 | 126 | 9 | 158 |



| Number of <br> surrounding <br> Hyper-boxes | Corresponding <br> Configurations <br> (see Appendix A) | Number of <br> surrounding <br> Hyper-boxes | Corresponding <br> Configurations <br> (see Appendix A) |  |
| :---: | :---: | :---: | :---: | :---: |
| 3 | 8 | 13 | 244 |  |
| 4 | 19 | 12 | 234 |  |
| 5 | 31 | 11 | 223 |  |
| 7 | 86 | 9 | 165 |  |
| 8 | 114 | 169 |  |  |
|  | 115 |  |  |  |



V3N4-3

| Number of <br> surrounding <br> Hyper-boxes | Corresponding <br> Configurations <br> (see Appendix A) |
| :---: | :---: |
| 7 | 99 |



| Number of <br> surrounding <br> Hyper-boxes | Corresponding <br> Configurations <br> (see Appendix A) | Number of <br> surrounding <br> Hyper-boxes | Corresponding <br> Configurations <br> (see Appendix A) |
| :---: | :---: | :---: | :---: |
| 6 | 54 | 10 | 189 |
|  | 58 |  | 194 |
| 8 | 122 | 9 | 155 |



V3N5-2

| Number of <br> surrounding <br> Hyper-boxes | Corresponding <br> Configurations <br> (see Appendix A) | Number of <br> surrounding <br> Hyper-boxes | Corresponding <br> Configurations <br> (see Appendix A) |
| :---: | :---: | :---: | :---: |
| 7 | 100 | 9 | 153 |



| Number of <br> surrounding <br> Hyper-boxes | Corresponding <br> Configurations <br> (see Appendix A) | Number of <br> surrounding <br> Hyper-boxes | Corresponding <br> Configurations <br> (see Appendix A) |
| :---: | :---: | :---: | :---: |
| 1 | 2 | 15 | 252 |
| 3 | 7 | 13 | 247 |
| 5 | 29 | 11 | 225 |
| 7 | 79 | 9 | 175 |



| Number of <br> surrounding <br> Hyper-boxes | Corresponding <br> Configurations <br> (see Appendix A) | Number of <br> surrounding <br> Hyper-boxes | Corresponding <br> Configurations <br> (see Appendix A) |
| :---: | :---: | :---: | :---: |
| 6 | 59 | 10 | 201 |



V4N1

| Number of <br> surrounding <br> Hyper-boxes | Corresponding <br> Configurations <br> (see Appendix A) | Number of <br> surrounding <br> Hyper-boxes | Corresponding <br> Configurations <br> (see Appendix A) |
| :---: | :---: | :---: | :---: |
| 3 | 11 | 13 | 245 |



| Number of <br> surrounding <br> Hyper-boxes | Corresponding <br> Configurations <br> (see Appendix A) | Number of <br> surrounding <br> Hyper-boxes | Corresponding <br> Configurations <br> (see Appendix A) |
| :---: | :---: | :---: | :---: |
| 2 | 4 | 14 | 250 |
| 6 | 50 | 12 | 235 |
|  |  | 10 | 204 |



V4N2-2

| Number of <br> surrounding <br> Hyper-boxes | Corresponding <br> Configurations <br> (see Appendix A) | Number of <br> surrounding <br> Hyper-boxes | Corresponding <br> Configurations <br> (see Appendix A) |
| :---: | :---: | :---: | :---: |
| 6 | 52 | 10 | 192 |



| Number of <br> surrounding <br> Hyper-boxes | Corresponding <br> Configurations <br> (see Appendix A) | Number of <br> surrounding <br> Hyper-boxes | Corresponding <br> Configurations <br> (see Appendix A) |
| :---: | :---: | :---: | :---: |
| 5 | 34 | 11 | 218 |
| 7 | 92 | 10 | 199 |



| Number of <br> surrounding <br> Hyper-boxes | Corresponding <br> Configurations <br> (see Appendix A) | Number of <br> surrounding <br> Hyper-boxes | Corresponding <br> Configurations <br> (see Appendix A) |
| :---: | :---: | :---: | :---: |
| 3 | 10 | 13 | 242 |
|  | 12 | 10 | 243 |
| 6 | 56 |  | 191 |
|  | 61 |  | 193 |
|  |  | 9 | 195 |
| 7 | 82 |  | 196 |
|  |  | 166 |  |



V4N4-2

| Number of <br> surrounding <br> Hyper-boxes | Corresponding <br> Configurations <br> (see Appendix A) | Number of <br> surrounding <br> Hyper-boxes | Corresponding <br> Configurations <br> (see Appendix A) |
| :---: | :---: | :---: | :---: |
| 6 | 74 | 10 | 181 |
| 7 | 93 |  |  |
| 8 | 121 |  |  |
|  | 123 |  |  |



V5

| Number of <br> surrounding <br> Hyper-boxes | Corresponding <br> Configurations <br> (see Appendix A) | Number of <br> surrounding <br> Hyper-boxes | Corresponding <br> Configurations <br> (see Appendix A) |
| :---: | :---: | :---: | :---: |
| 4 | 15 | 12 | 239 |



V5-2

| Number of <br> surrounding <br> Hyper-boxes | Corresponding <br> Configurations <br> (see Appendix A) | Number of <br> surrounding <br> Hyper-boxes | Corresponding <br> Configurations <br> (see Appendix A) |
| :---: | :---: | :---: | :---: |
| 7 | 80 | 9 | 173 |
|  | 84 |  | 174 |



V5N2

| Number of <br> surrounding <br> Hyper-boxes | Corresponding <br> Configurations <br> (see Appendix A) | Number of <br> surrounding <br> Hyper-boxes | Corresponding <br> Configurations <br> (see Appendix A) |
| :---: | :---: | :---: | :---: |
| 4 | 22 | 12 | 236 |
| 8 | 117 |  |  |



V5N2-2

| Number of <br> surrounding <br> Hyper-boxes | Corresponding <br> Configurations <br> (see Appendix A) |
| :---: | :---: |
| 6 | 57 |
|  | 60 |



| Number of <br> surrounding <br> Hyper-boxes | Corresponding <br> Configurations <br> (see Appendix A) | Number of <br> surrounding <br> Hyper-boxes | Corresponding <br> Configurations <br> (see Appendix A) |
| :---: | :---: | :---: | :---: |
| 5 | 37 | 11 | 219 |
| 8 |  |  | 220 |



V6

| Number of <br> surrounding <br> Hyper-boxes | Corresponding <br> Configurations <br> (see Appendix A) |
| :---: | :---: |
| 5 | 38 |
| 8 | 112 |



| Number of <br> surrounding <br> Hyper-boxes | Corresponding <br> Configurations <br> (see Appendix A) | Number of <br> surrounding <br> Hyper-boxes | Corresponding <br> Configurations <br> (see Appendix A) |  |
| :---: | :---: | :---: | :---: | :---: |
| 2 | 5 | 14 | 249 |  |
| 6 | 51 |  |  |  |
| 8 | 118 |  |  |  |



V6N1-2

| Number of <br> surrounding <br> Hyper-boxes | Corresponding <br> Configurations <br> (see Appendix A) |
| :---: | :---: |
| 9 | 167 |



| Number of <br> surrounding <br> Hyper-boxes | Corresponding <br> Configurations <br> (see Appendix A) | Number of <br> surrounding <br> Hyper-boxes | Corresponding <br> Configurations <br> (see Appendix A) |
| :---: | :---: | :---: | :---: |
| 7 | 81 | 12 | 237 |
|  | 83 |  |  |
| 8 | 101 | 9 | 170 |
|  | 129 |  | 171 |



V7

| Number of <br> surrounding <br> Hyper-boxes | Corresponding <br> Configurations <br> (see Appendix A) | Number of <br> surrounding <br> Hyper-boxes | Corresponding <br> Configurations <br> (see Appendix A) |
| :---: | :---: | :---: | :---: |
| 4 | 14 | 12 | 240 |
| 8 | 111 | 11 | 221 |
|  |  | 10 | 203 |



| Number of <br> surrounding <br> Hyper-boxes | Corresponding <br> Configurations <br> (see Appendix A) |
| :---: | :---: |
| 7 | 85 |



| V8 |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Number of <br> surrounding <br> Hyper-boxes | Corresponding <br> Configurations <br> (see Appendix A) | Number of <br> surrounding <br> Hyper-boxes | Corresponding <br> Configurations <br> (see Appendix A) |  |  |
| 2 | 6 | 14 | 248 |  |  |
| 5 | 32 | 11 | 222 |  |  |
| 6 | 55 | 10 | 202 |  |  |
| 8 | 110 |  |  |  |  |

